

Fermi liquid and beyond in Sr_2RuO_4

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Antonio Vecchione - *Universita di Salerno*

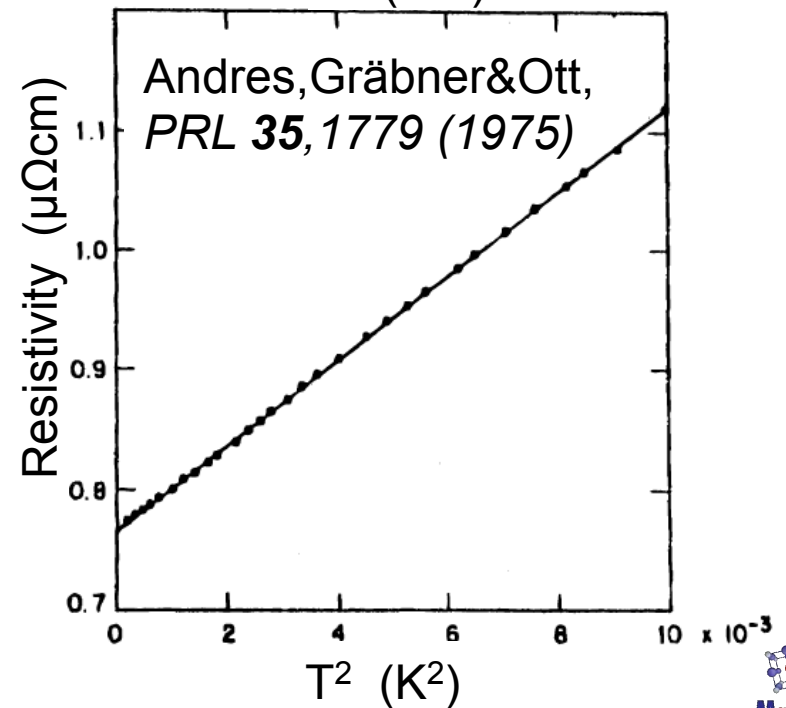
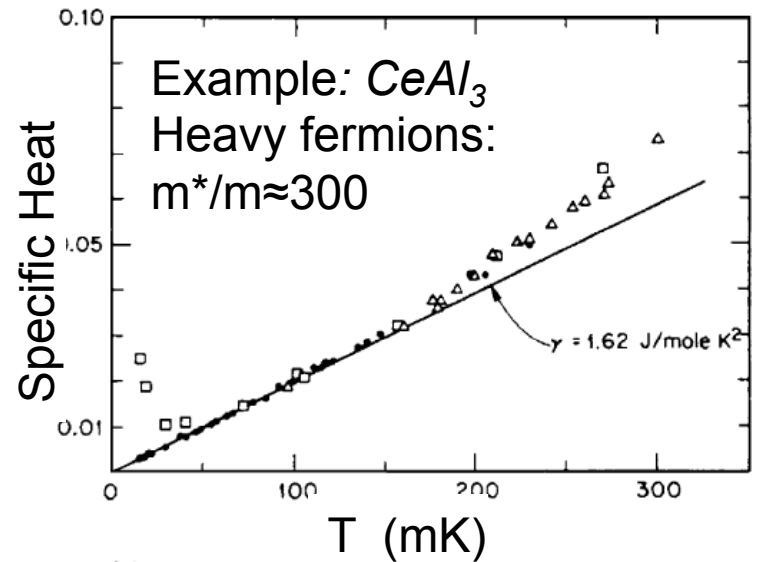
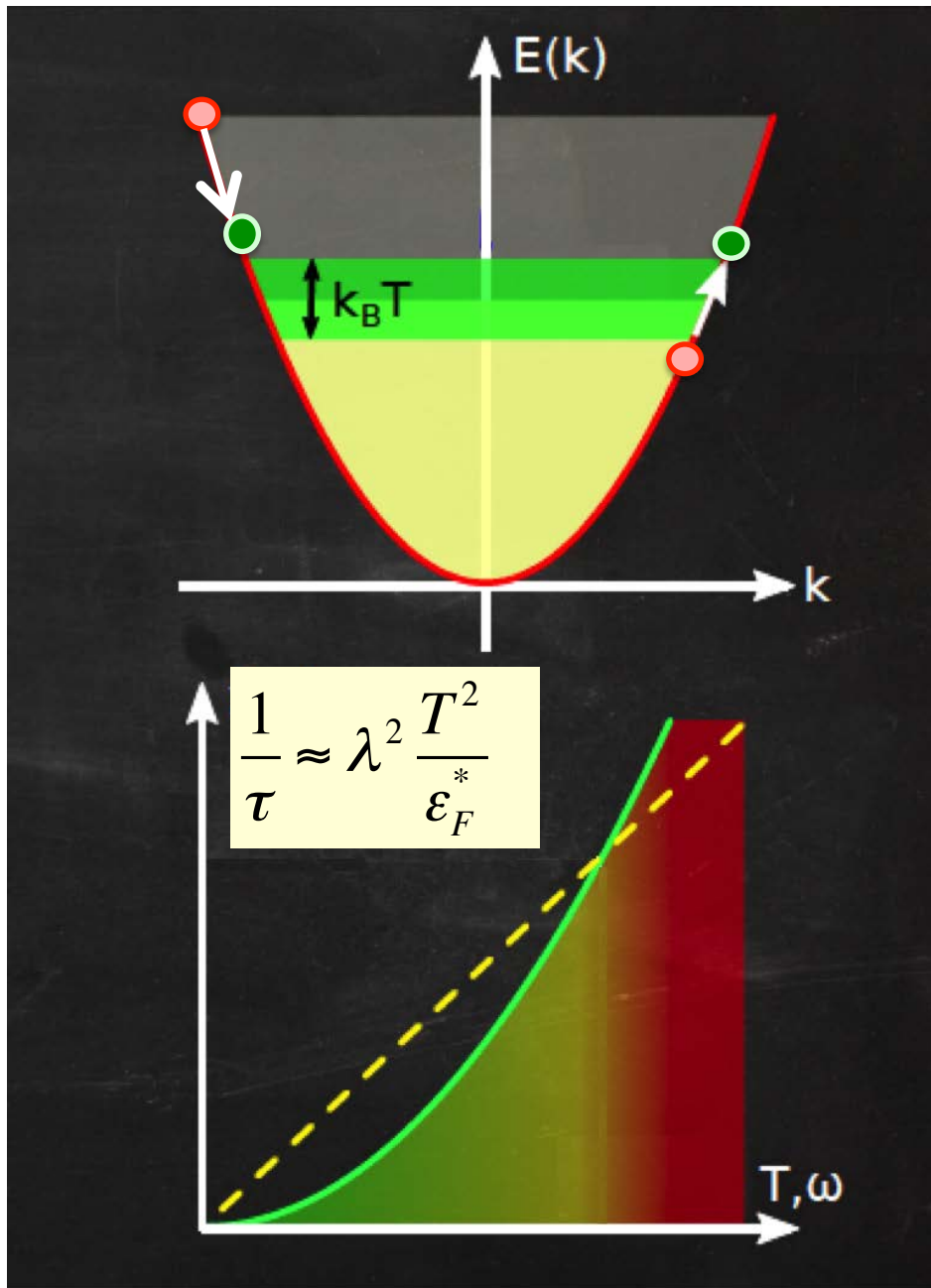


Antoine Georges - *EcoPoly Palaisau, UniGenève & Collège de France*

Dirk van der Marel - *Université de Genève*

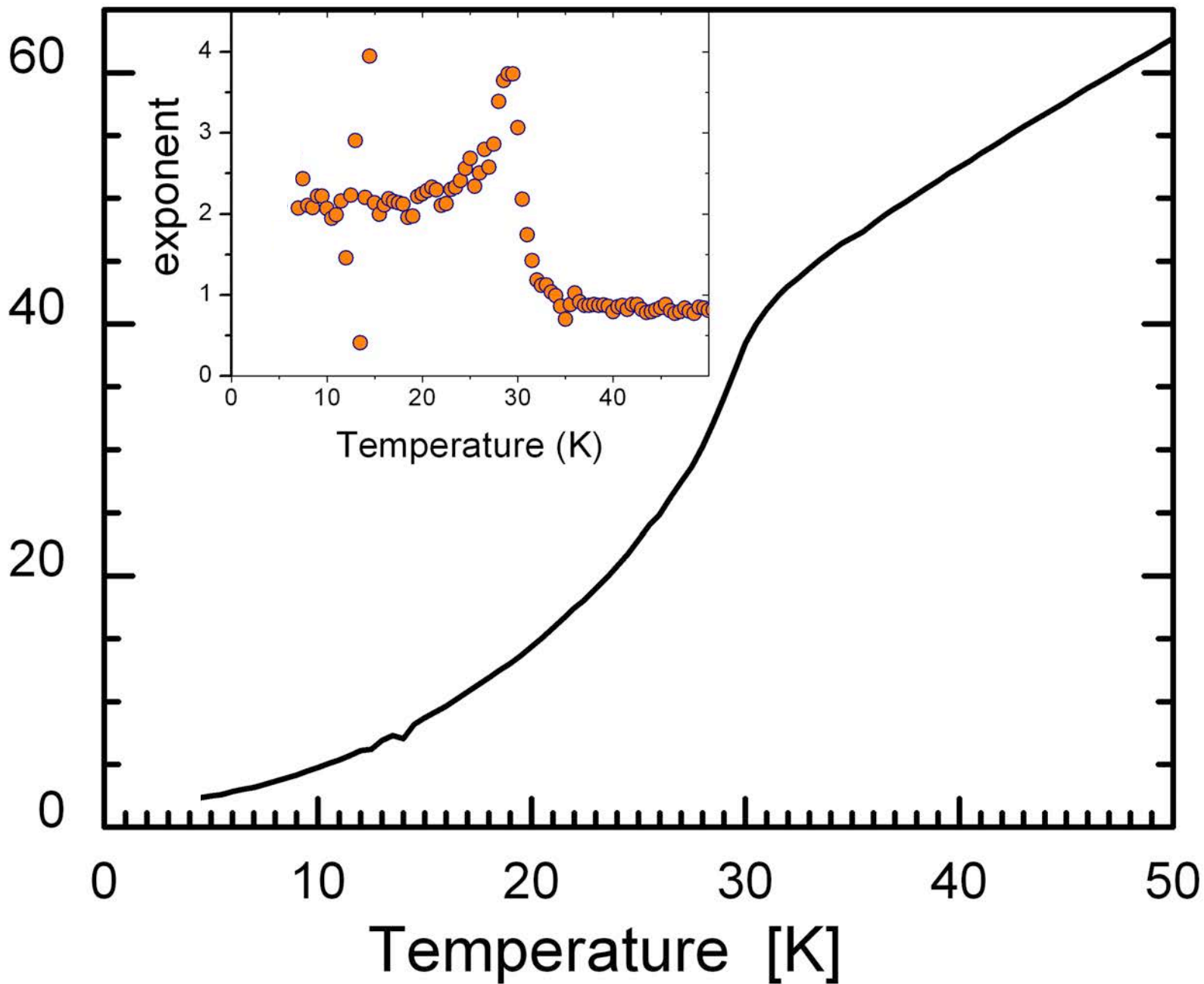
SCSR2014 Adriatico Guesthouse, Trieste, 10-11 December 2014

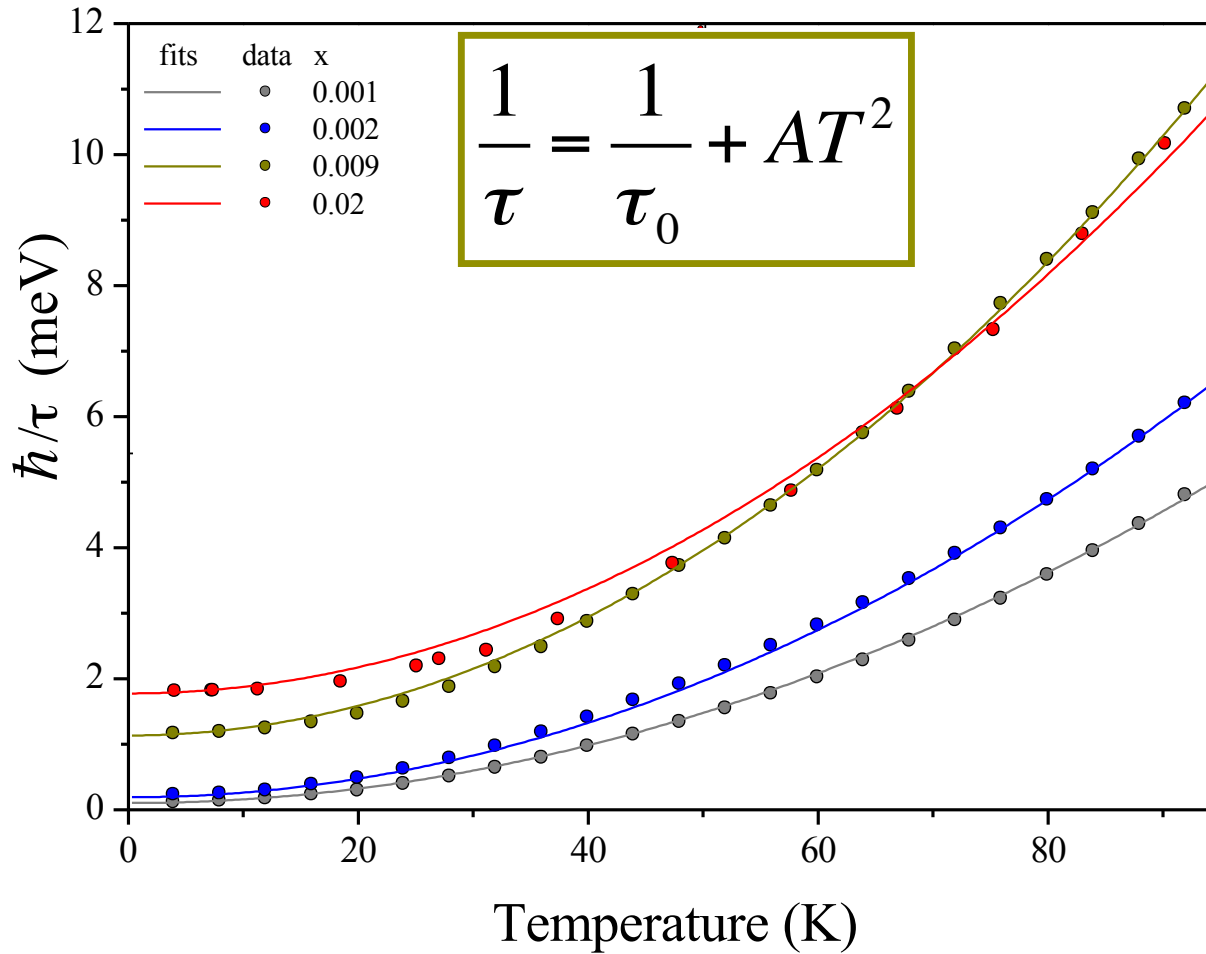
Landau-Fermi liquids



MnSi

$\rho(T)$ [$\mu\Omega\text{cm}$]





DvdM, I. I. Mazin, J.L.M. van Mechelen, *PRB* **84**, 205111 (2011)

Three questions :

- How do we tell it's a Fermi Liquid when we see one (in optics) ?
- Can we understand the Non Fermi-Liquid behavior in Sr_2RuO_4 above ~ 0.1 eV ?
- What does it teach us about the physics of Sr_2RuO_4 ?

How do we tell it's a FL ?

- The simple answer -

Single-particle
Lifetime :

$$\frac{1}{\tau_{qp}} \propto (\hbar\omega)^2 + (\pi k_B T)^2$$

Two-particle:

$$\frac{1}{\tau_{opt}} \propto (\hbar\omega)^2 + (2\pi k_B T)^2 \quad (\hbar\omega \geq \pi k_B T)$$

R. N. Gurzhi, Sov. Phys. JETP 35, 673 (1959)

D. L. Maslov & A. V. Chubukov, PRB 86, 155137 (2012)

C. Berthod *et al*, PRB 87, 115109 (2013)

Strangely enough, this precise form (including factor 2π)
was not experimentally demonstrated from optics until now !

Some questions to be answered about $1/\tau_{opt}(\omega, T)$

1a) $\tau_{opt}^{-1}(\omega, T) = \tau_{opt}^{-1}(\omega, 0) + A(pk_B T)^\mu$?

b) What is the value of μ ?

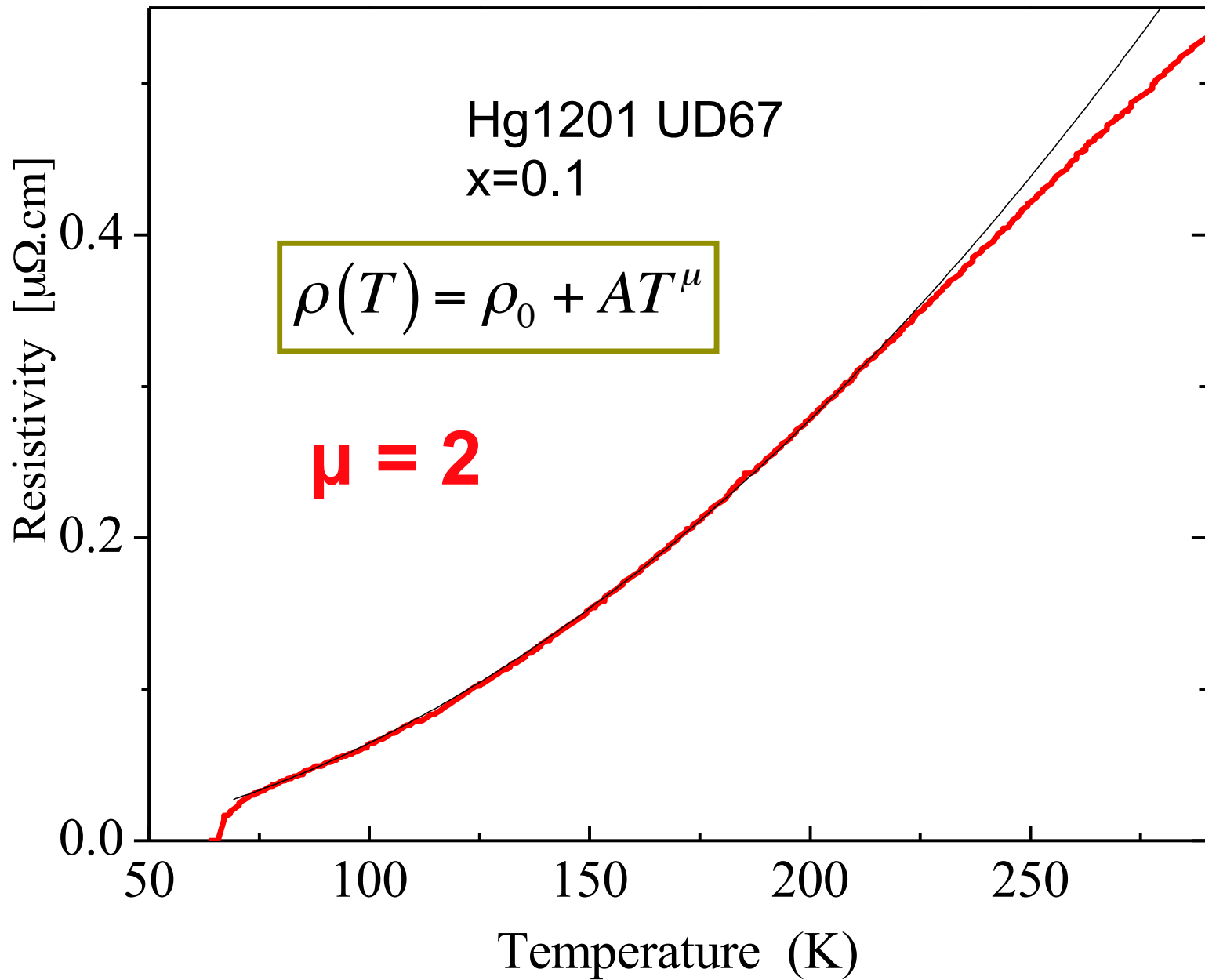
2a) $\tau_{opt}^{-1}(\omega, T) = \tau_{opt}^{-1}(0, T) + A(\hbar\omega)^\eta$?

b) What is the value of η ?

3a) $\left\{ \begin{array}{l} \tau_{opt}^{-1}(\omega, T) = f(\xi) \\ \xi = \sqrt{(\hbar\omega)^2 + (pk_B T)^2} \end{array} \right\}$?

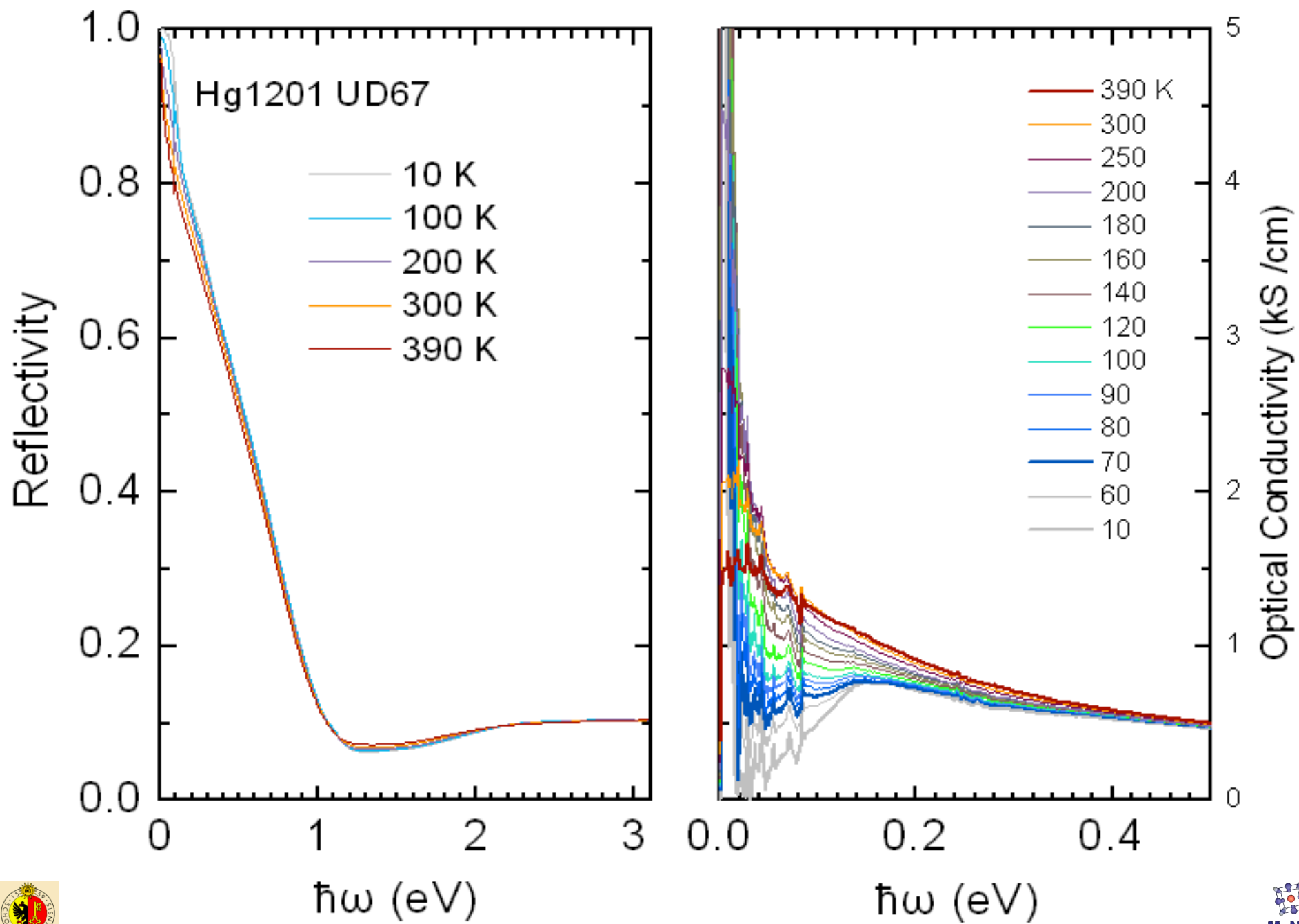
b) What is the value of p ?





N Barisic *et al.*, *PNAS* 2013
S.I. Mirzaei, D. Stricker *et al.*, *PNAS* 2013

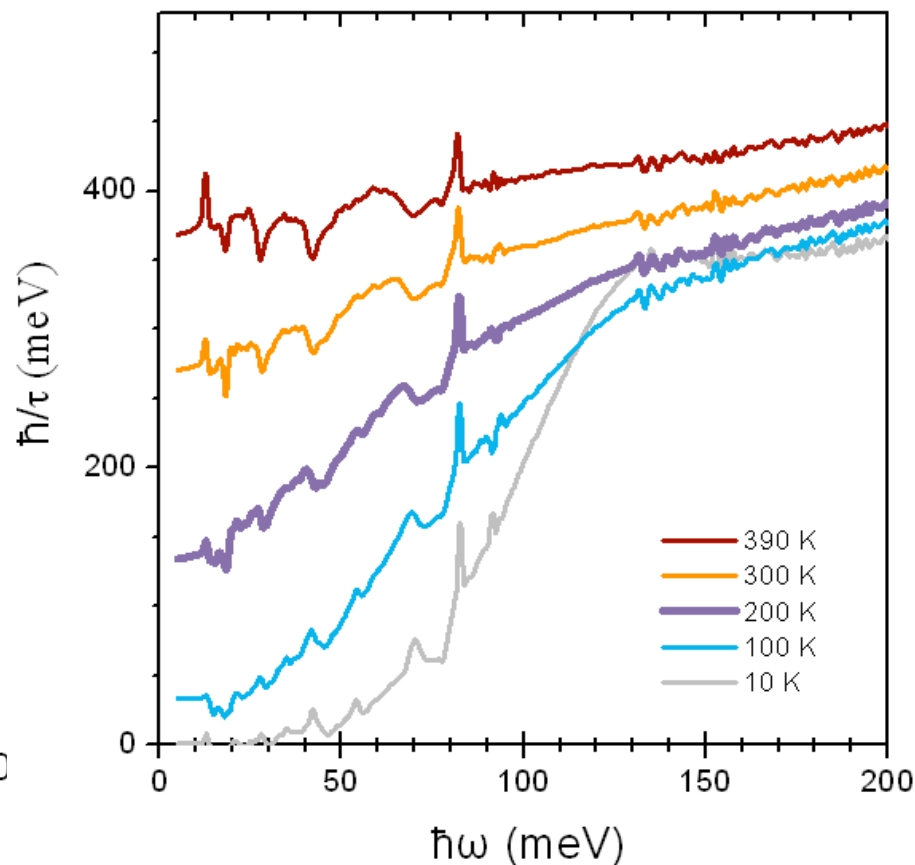
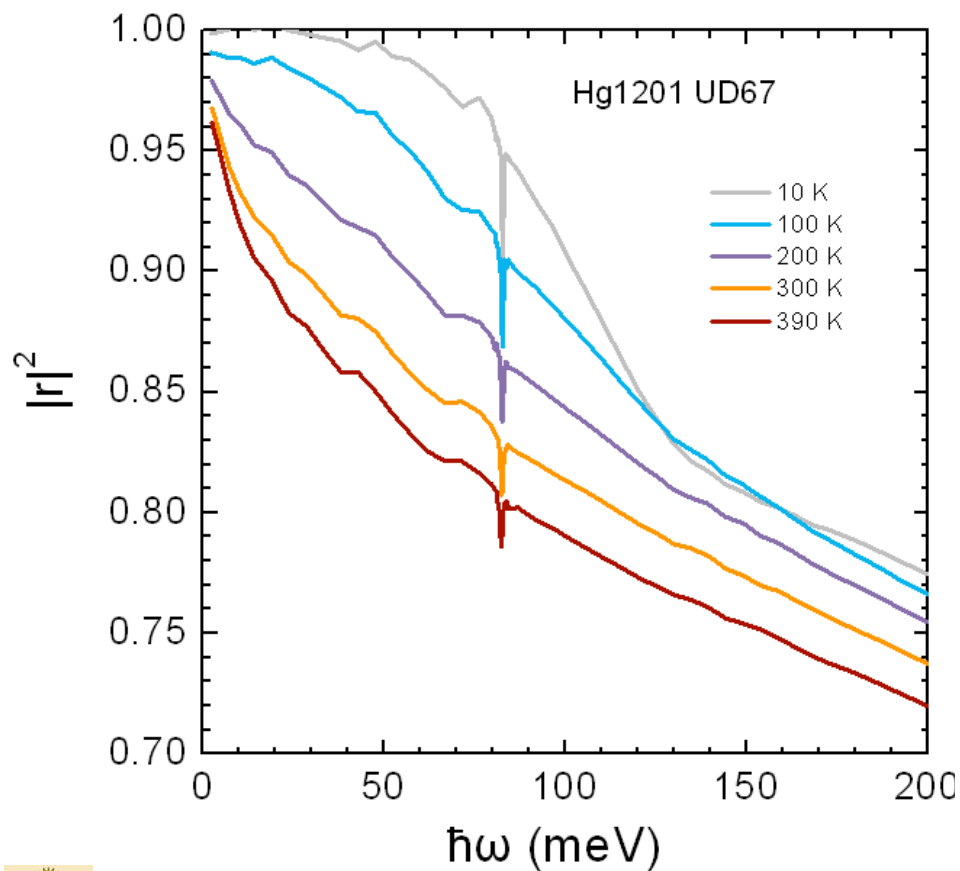
Hg1201 UD67



HgBa₂CuO₄: Energy dependend Relaxation rate

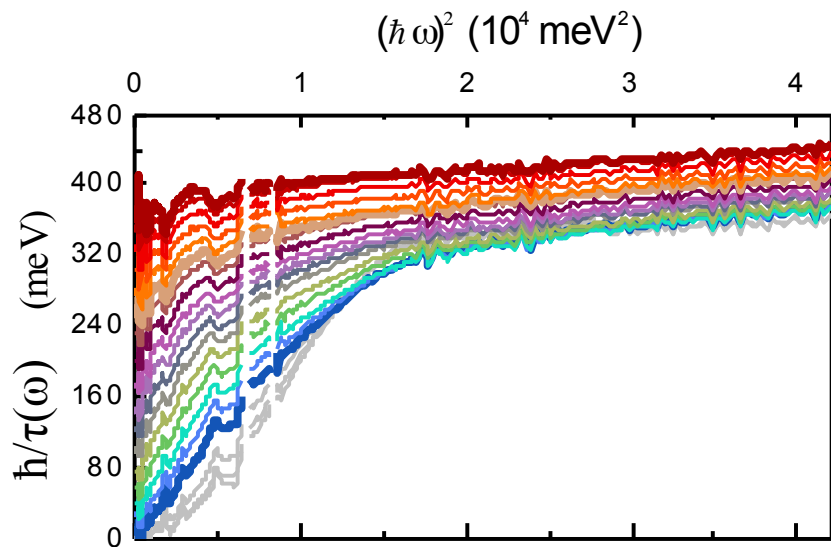
$$\text{Im} \frac{\omega_p^2 \omega^{-1}}{(1+r)^2 / (1-r)^2 - \epsilon_{bc}} = \frac{1}{\tau_{opt}(\omega)}$$

Basov, Averitt, vdMarel,
Dressel & Haule
RMP **83**, 471 (2011)



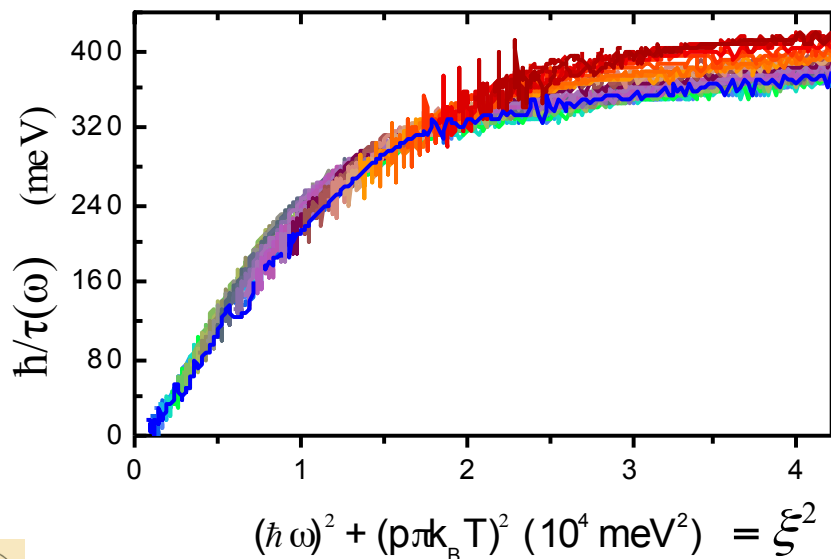
Fermi-liquid

Optical signature: scaling collapse



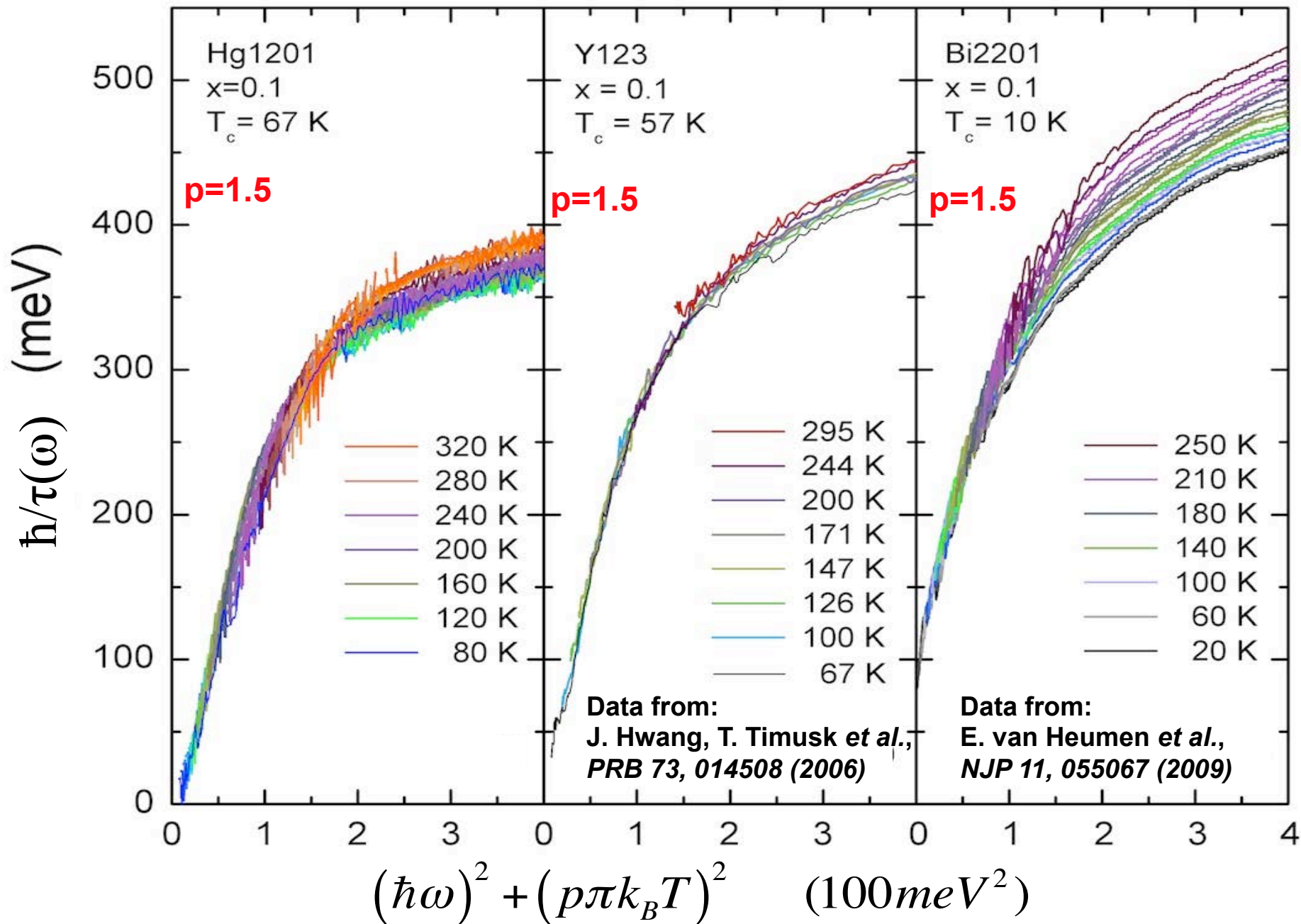
$$\frac{1}{\tau_{opt}} = \frac{1}{\tau(T)} + A\omega^\eta$$

$$\eta = 2$$



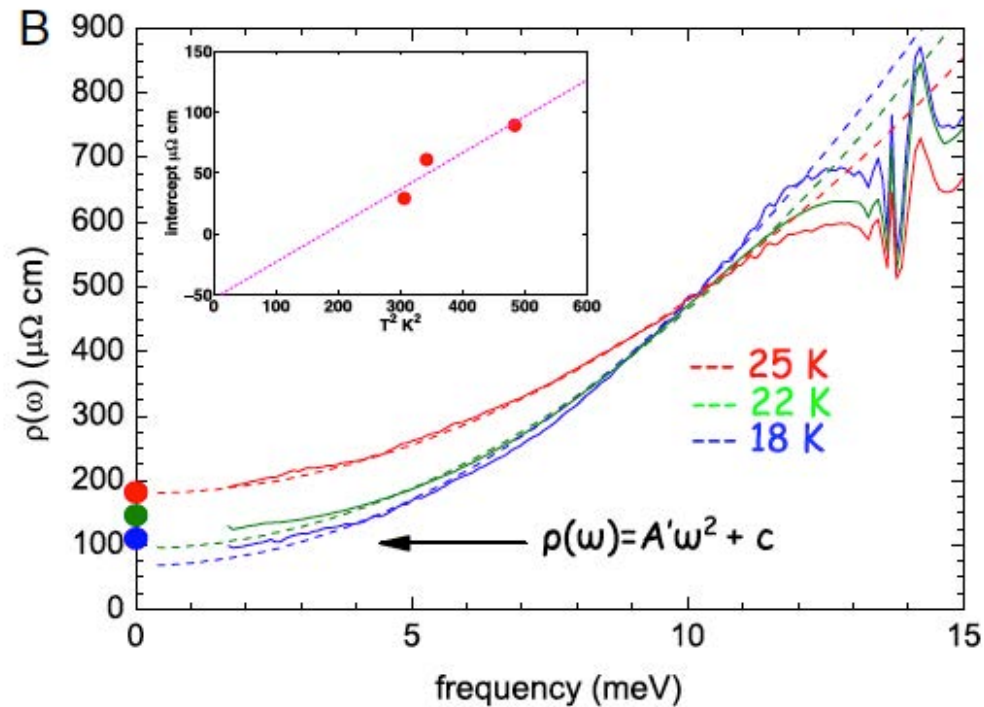
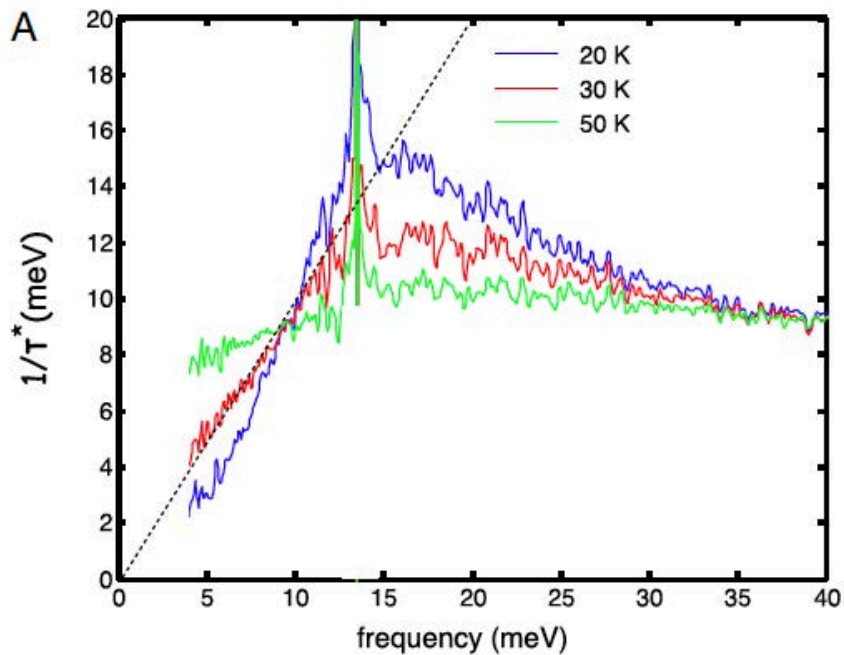
$$\frac{1}{\tau_{opt}} \propto (\hbar\omega)^2 + (p\pi k_B T)^2$$

$$p = 1.5$$



S.I. Mirzaei, D. Stricker *et al.*, *PNAS* 110, 5774 (2013)

URu₂Si₂



U. Nagel et al., *PNAS* 109,1916 (2012)

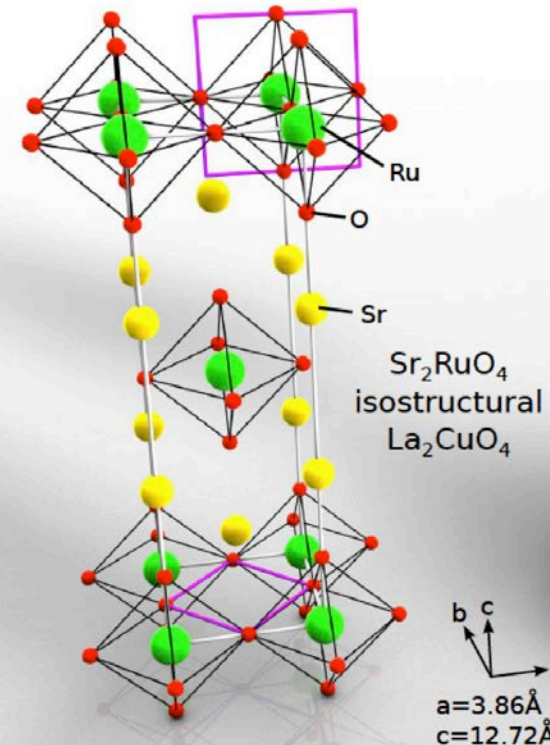
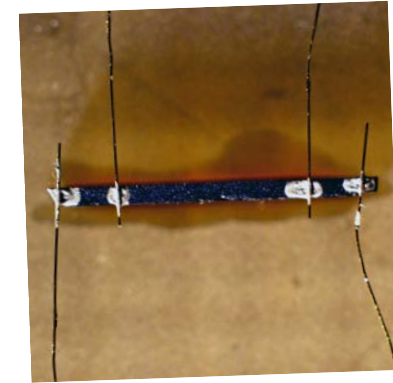
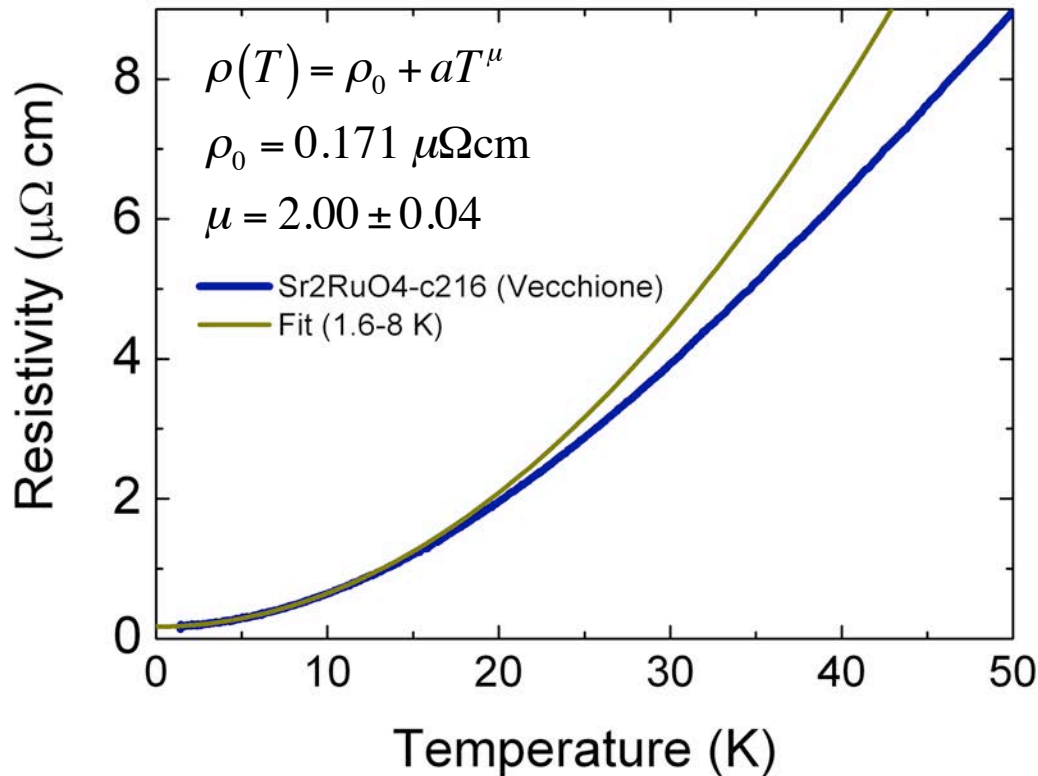
$$\frac{1}{\tau_{opt}} \propto (\hbar\omega)^2 + \mathbf{b} (\pi k_B T)^2 \quad \mathbf{b} = \mathbf{p}^2 = \mathbf{1}$$

D. L. Maslov & A. V. Chubukov, *PRB* 86, 155137 (2012)

Explanation for $\mathbf{p}=1$: $1/\tau(\omega, T) = (2-\mathbf{p}^2)/\tau_{FL}(\omega, T) + 2\mathbf{p}^2/\tau_M(\omega)$

$1/\tau_M(\omega)$: Unitary scattering (magnetic impurities)

Sr_2RuO_4 : the 'Helium 3' of transition-metal oxides !

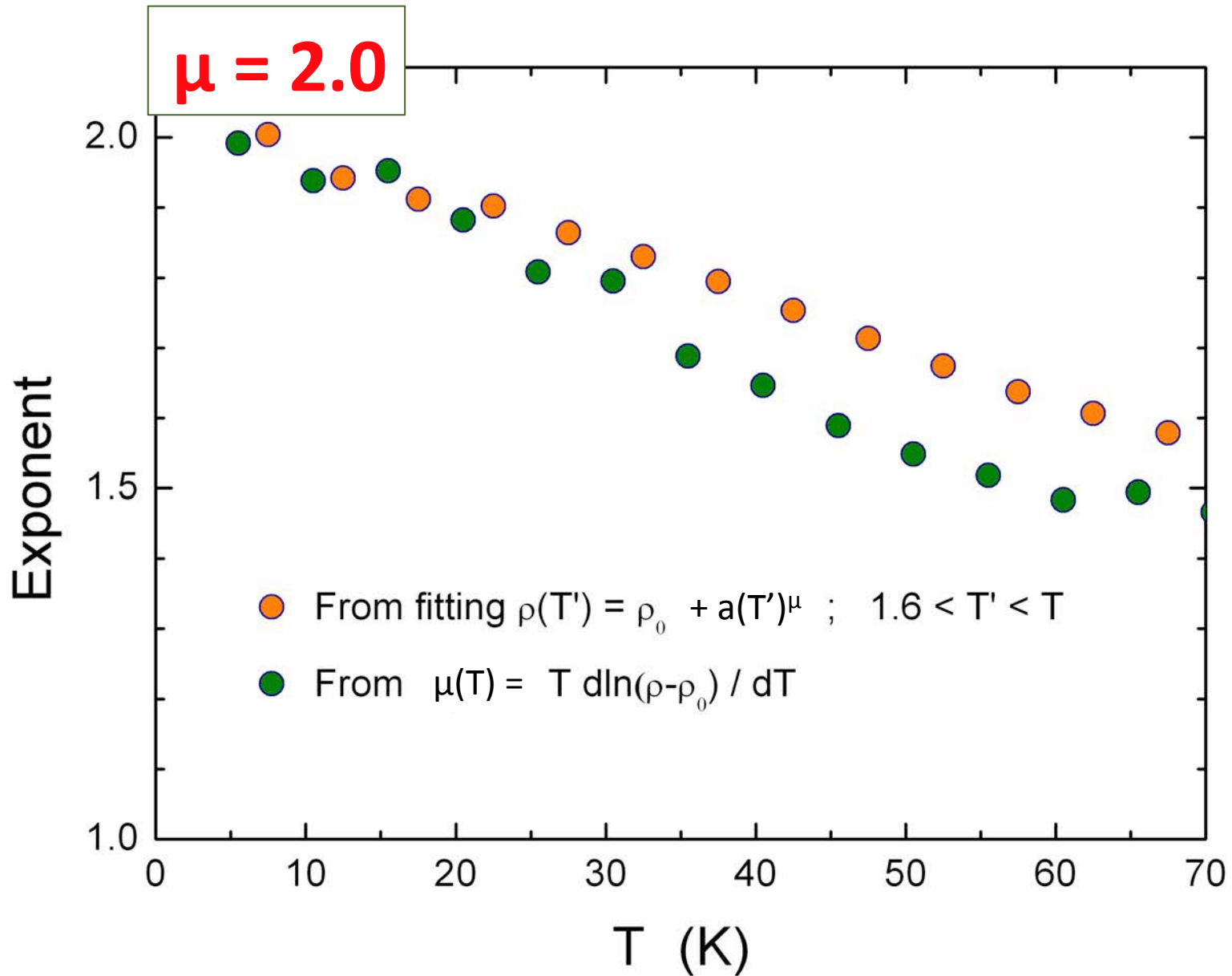


Beautiful review articles:

- A.Mackenzie & Y.Maeno, RMP 75 ,657 (2003)
- Bergemann, Adv. Phys. 52, 639 (2003)

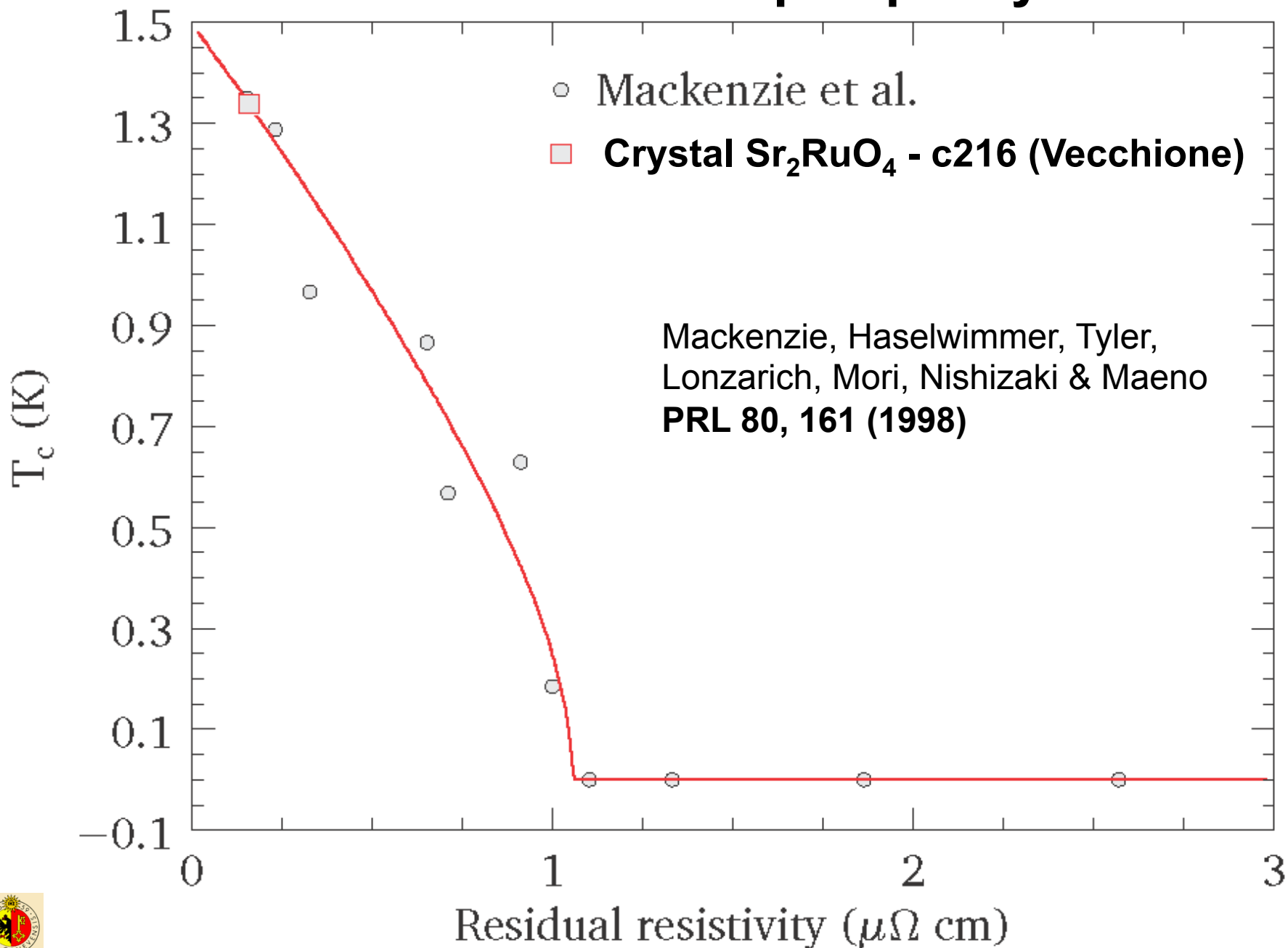


Ab-plane resistivity exponent

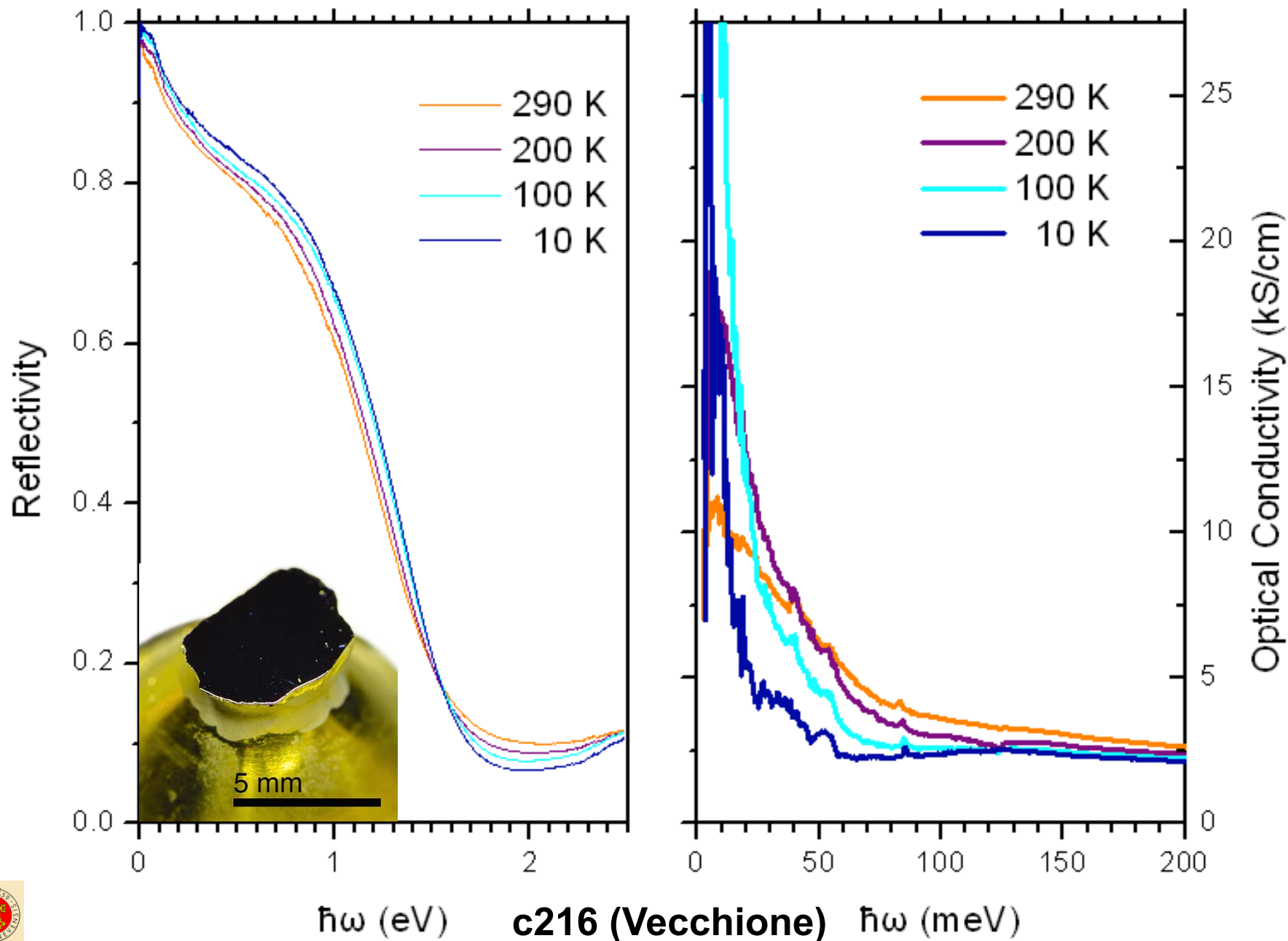


Crystal Sr_2RuO_4 - c216 (Vecchione)

Relative sample quality



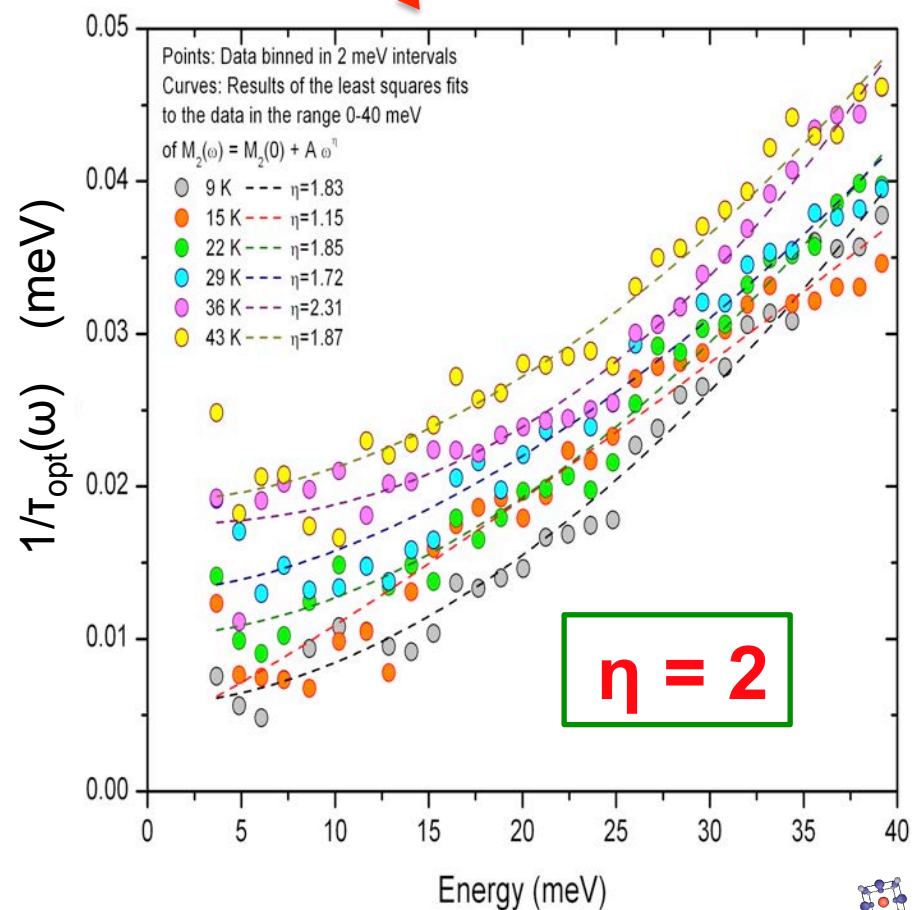
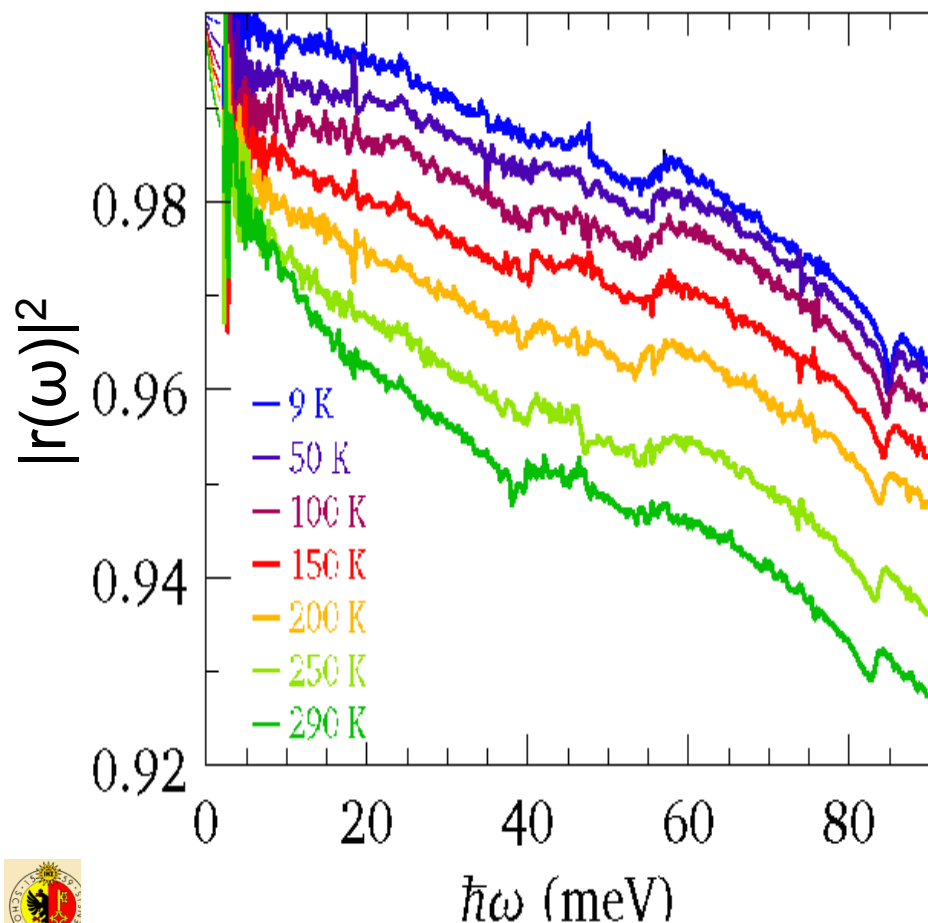
Ab-plane reflectivity of Sr_2RuO_4



Sr₂RuO₄: Energy dependent Relaxation rate

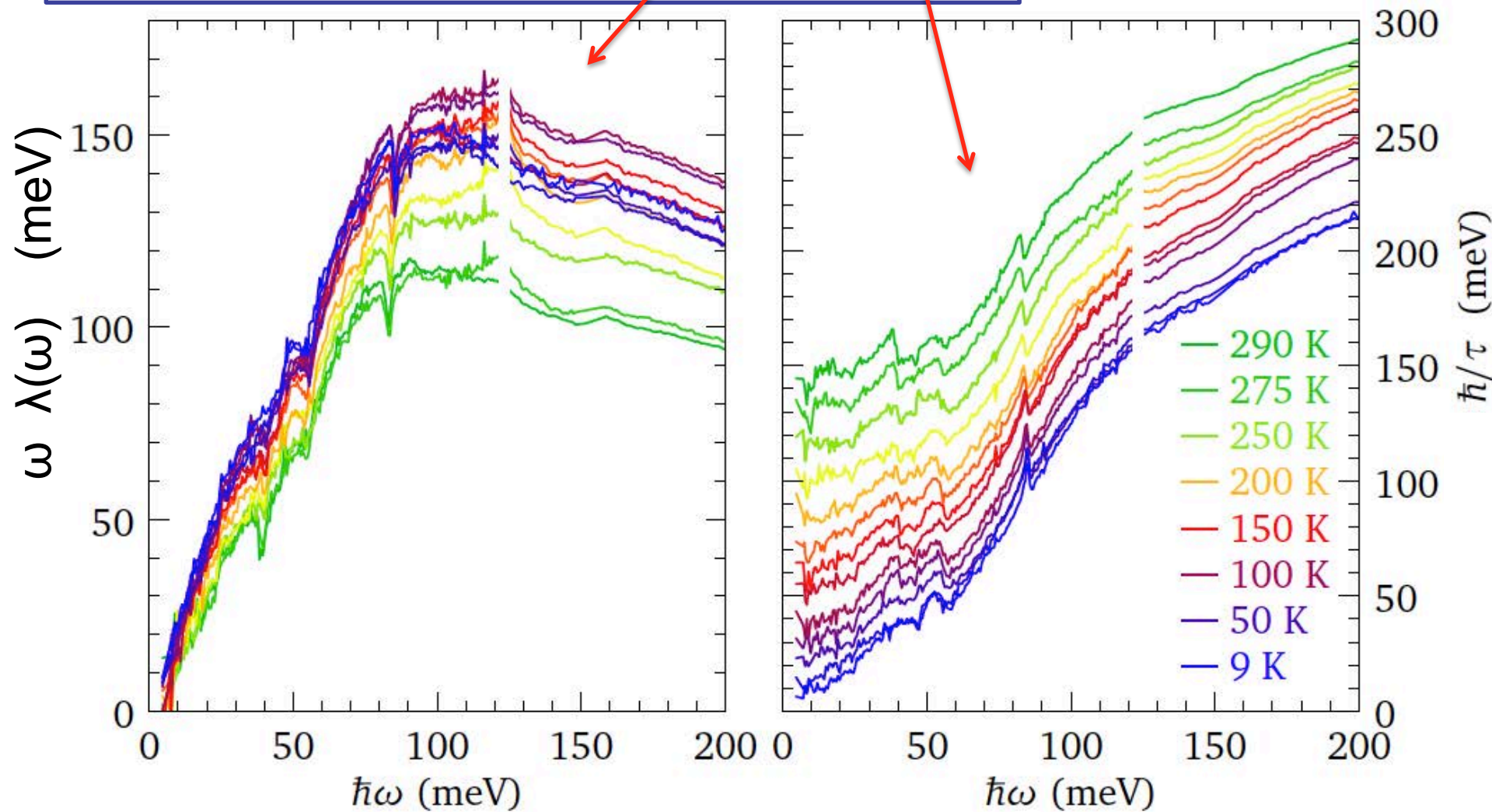
$$\text{Im} \frac{\omega_p^2 \omega^{-1}}{(1+r)^2 / (1-r)^2 - \epsilon_{bc}} = \frac{1}{\tau_{opt}(\omega)}$$

Basov, Averitt, vdMarel,
Dressel & Haule
RMP **83**, 471 (2011)



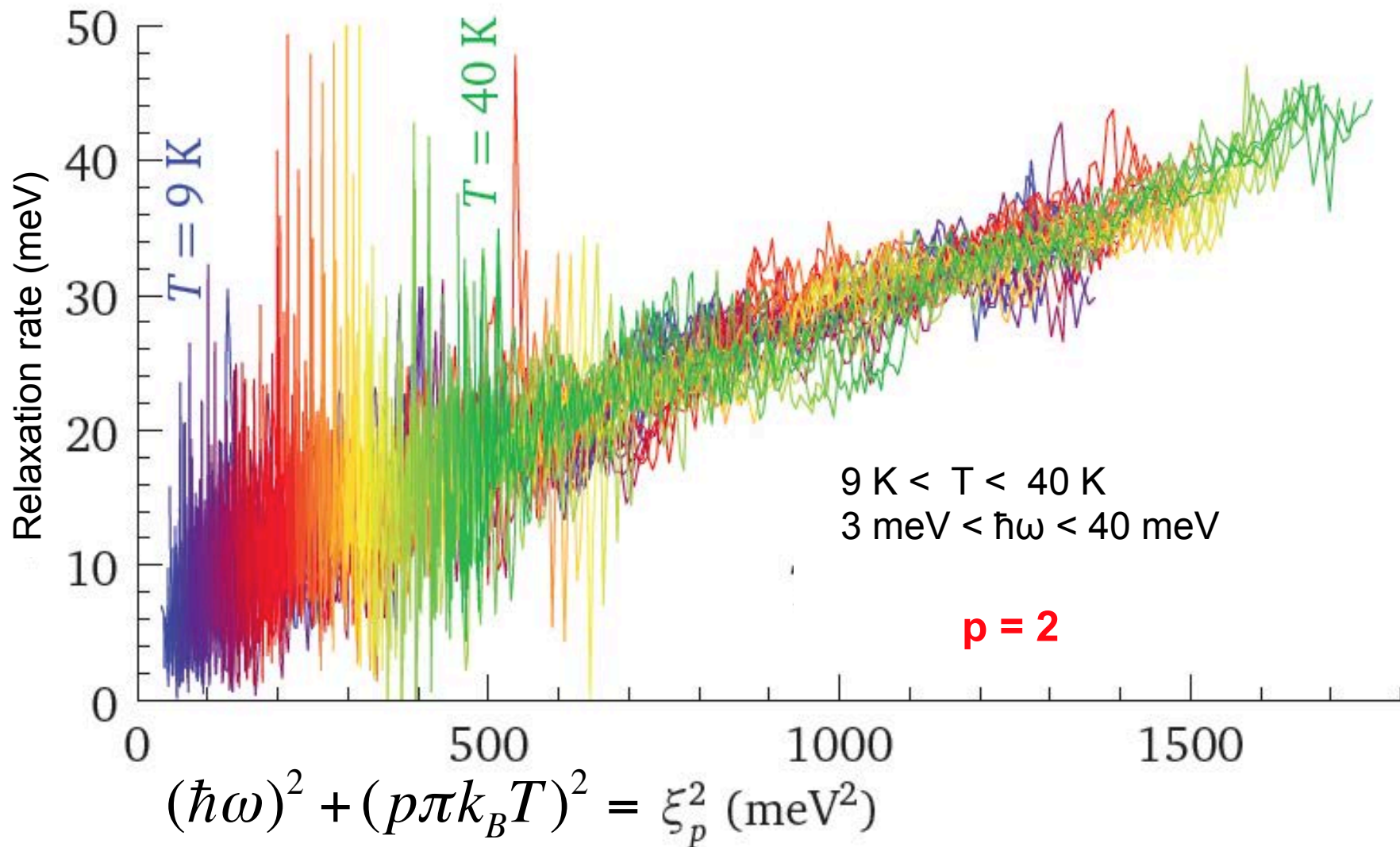
Sr₂RuO₄: Mass renormalization and relaxation rate

$$\frac{\omega_p^2 \omega^{-1}}{(1+r)^2 / (1-r)^2 - \epsilon_{bc}} = \omega \left[1 + \lambda_{opt}(\omega) \right] + \frac{i}{\tau_{opt}(\omega)}$$



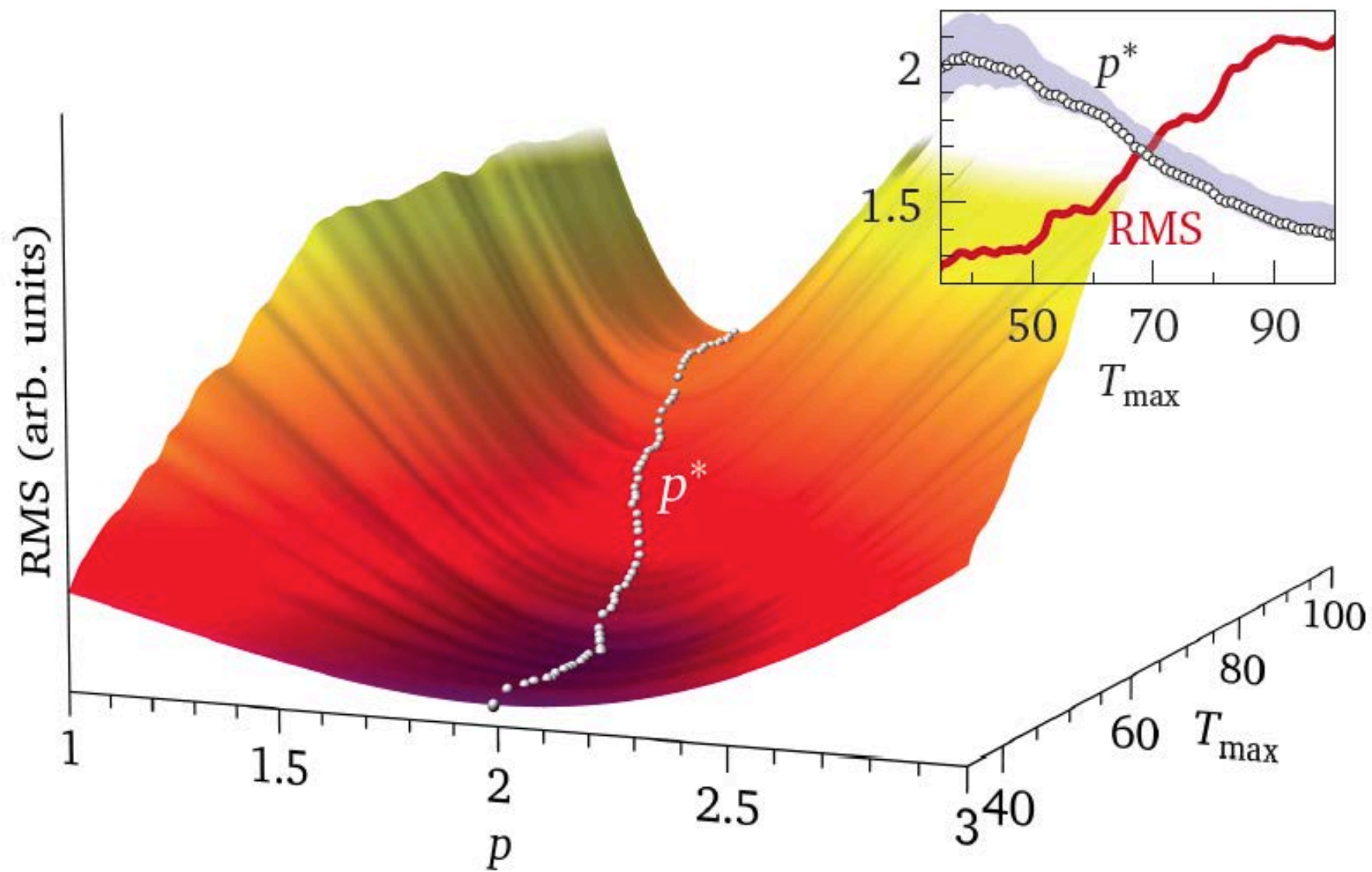
Crystal Sr₂RuO₄ - c216 (Vecchione)

Sr₂RuO₄: Scaling collapse



Crystal Sr₂RuO₄ - c216 (Vecchione)

Sr_2RuO_4 : Scaling collapse



Crystal Sr_2RuO_4 - c216 (Vecchione)

Some questions that we have answered about $1/\tau_{opt}(\omega, T)$

1a) $\tau_{opt}^{-1}(\omega, T) = \tau_{opt}^{-1}(\omega, 0) + A(pk_B T)^\mu$ Affirmative

b) $\mu \approx 2$

2a) $\tau_{opt}^{-1}(\omega, T) = \tau_{opt}^{-1}(0, T) + A(\hbar\omega)^\eta$ Affirmative

b) $\eta \approx 2$

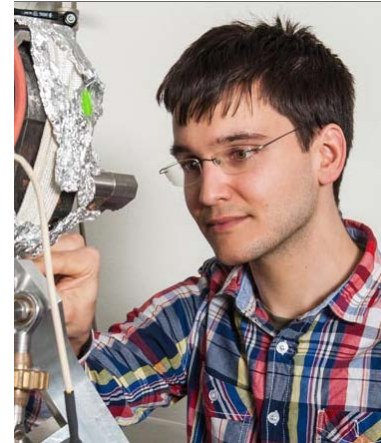
3a) $\left\{ \begin{array}{l} \tau_{opt}^{-1}(\omega, T) = f(\xi) \\ \xi = \sqrt{(\hbar\omega)^2 + (pk_B T)^2} \end{array} \right\}$ Affirmative

b) $p \approx 2$



Some questions that we have answered
about the relaxation rate

$$1 / \tau_{opt}(\omega, T) \propto (\hbar\omega)^2 + (2\pi k_B T)^2$$



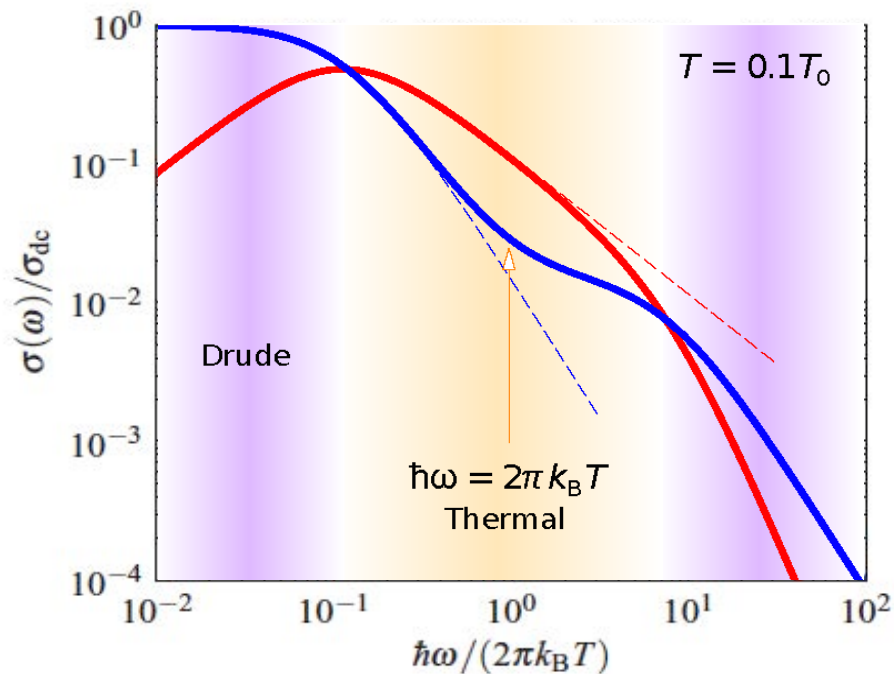
Damien Stricker

This confirms, that Sr_2RuO_4 is the solid
state analogue of ^3He

Stricker, Mravlje, Berthod, Fittipaldi, Vecchione, Georges, vdMarel,
PRL 113, 087404 (2014)

Universal scaling function (local FL)

$$\frac{\sigma(\omega, T)}{\sigma_{DC}} = F \left[\frac{\hbar\omega}{k_B T}, \frac{\hbar\omega T_0}{k_B T^2} \right]$$

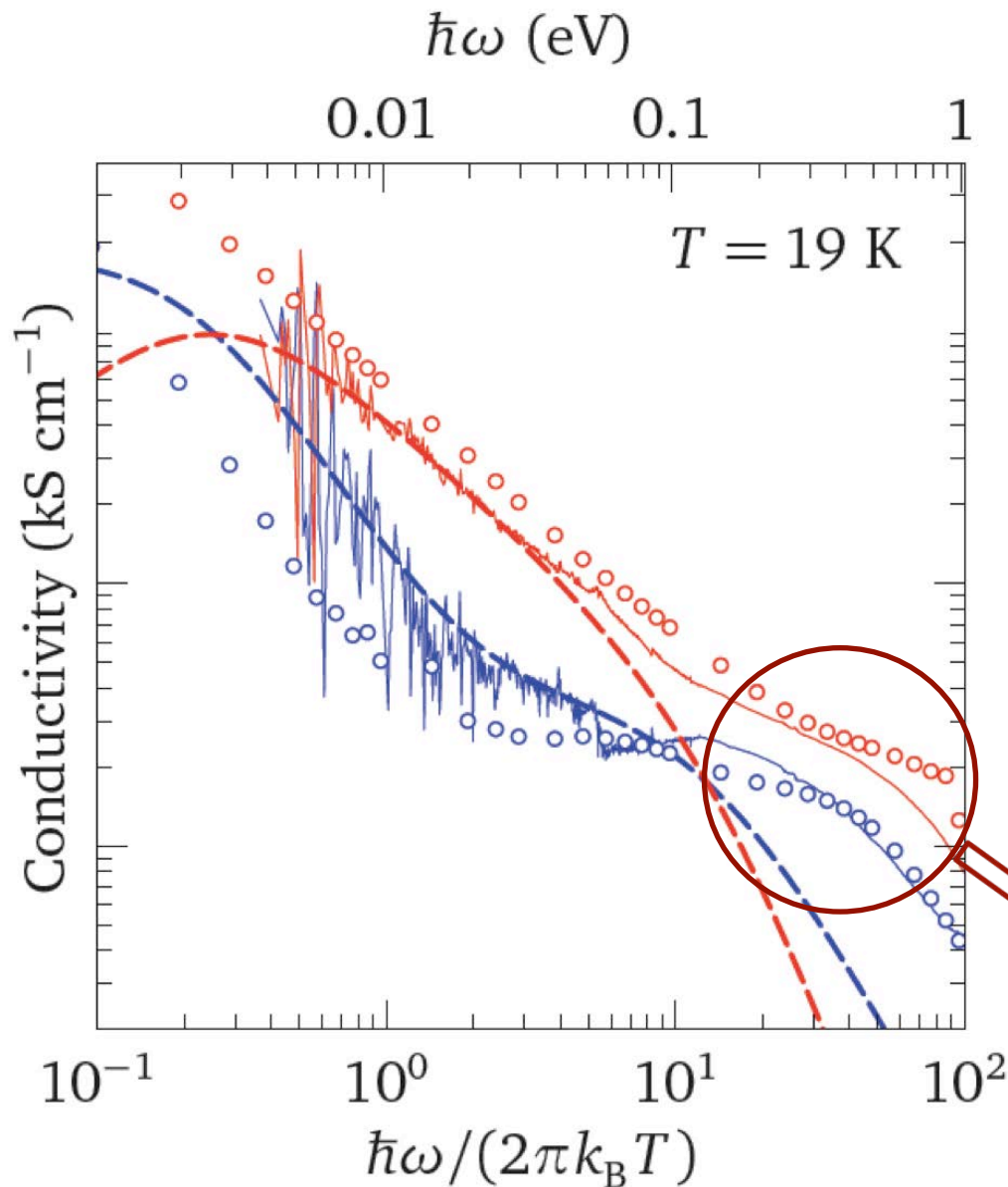


Signature of Fermi Liquid
is a DEVIATION from Drude's
formula, signalling frequency
dependence of the relaxation
rate

$$F[x, y] = \frac{6}{\pi^2 x} \int_{-\infty}^{\infty} du \frac{\left[e^{\pi(u-x)} + 1 \right]^{-1} - \left[e^{\pi(u+x)} + 1 \right]^{-1}}{1 + x^2 - iy + u^2}$$

C. Berthod, J.Mravlje, X. Deng, R. Žitko, D.van der Marel, and A. Georges,
PRB 87, 115109 (2013)

Re $\sigma(\omega)$ + i Im $\sigma(\omega)$



Plain Lines:

Experiments, Sr_2RuO_4

Dashed lines :

universal FL form

→ Beautiful agreement

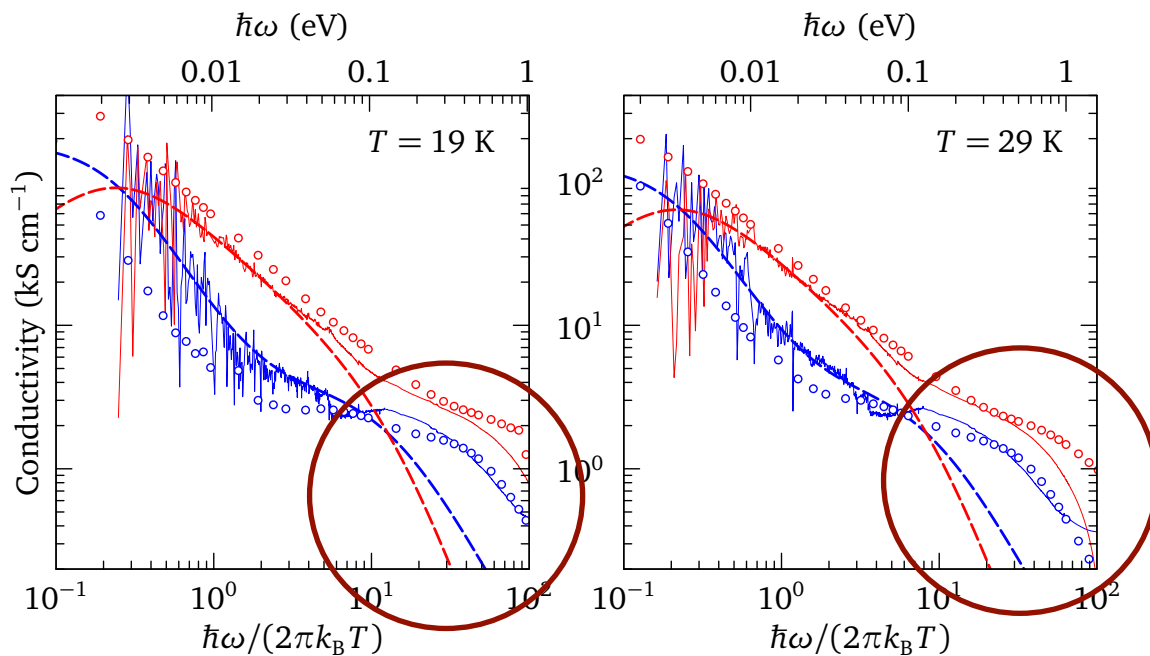
→ At low T , low ω

Dots:

LDA+DMFT
calculation for this
material

Clear deviations from
FL for ω above $\sim 0.1 \text{ eV}$
Very well described
by DMFT !

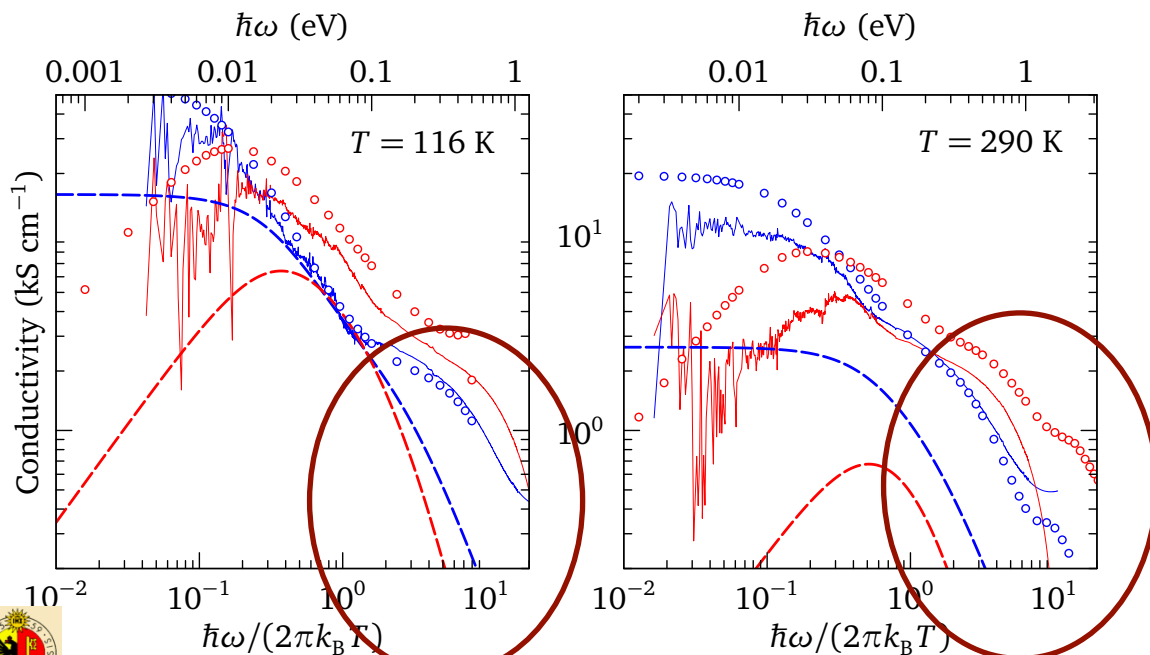
Re $\sigma(\omega)$ + i Im $\sigma(\omega)$



Plain Lines:
Experiments

Dashed lines :
universal FL form

Dots:
LDA+DMFT

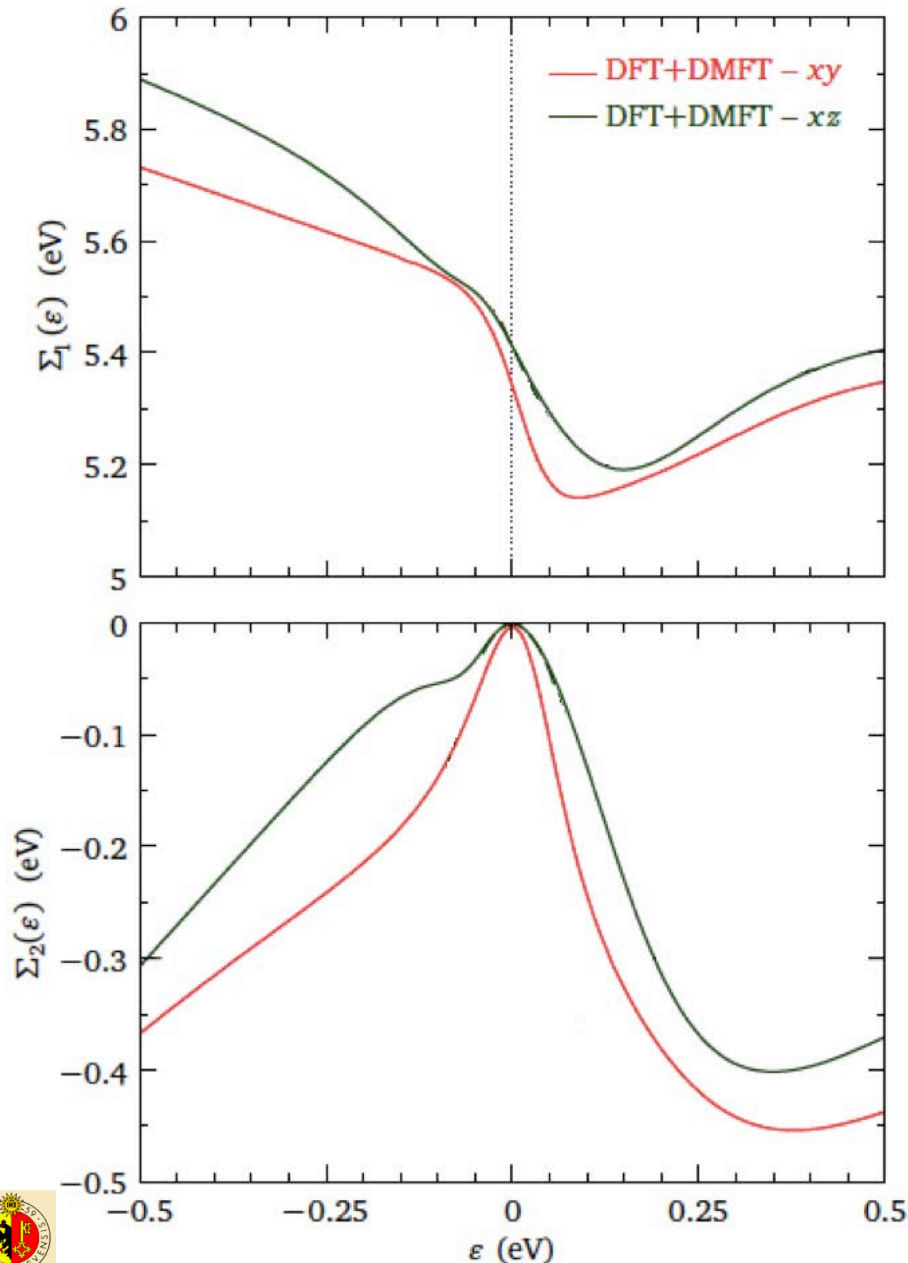


Clear deviations from
FL for ω above $\sim 0.1 \text{ eV}$
Very well described
by DMFT !

Beyond the Fermi Liquid regime: insights from DMFT

Mravlje, Georges et al., PRL 106, 096401 (2011)

Deng, Georges et al., PRL 110, 086401 (2012)



Real part of self-energy

Has a marked change of behavior at positive excitation energy, i.e. the effective mass decreases at high energy

Imaginary part of self-energy

The relaxation rate tends to saturate at high energy. It therefore stays below its extrapolated value from FLT

Hence, well above T_{FL} , well-defined single-particle excitations ('resilient quasiparticles') continue to exist, which:

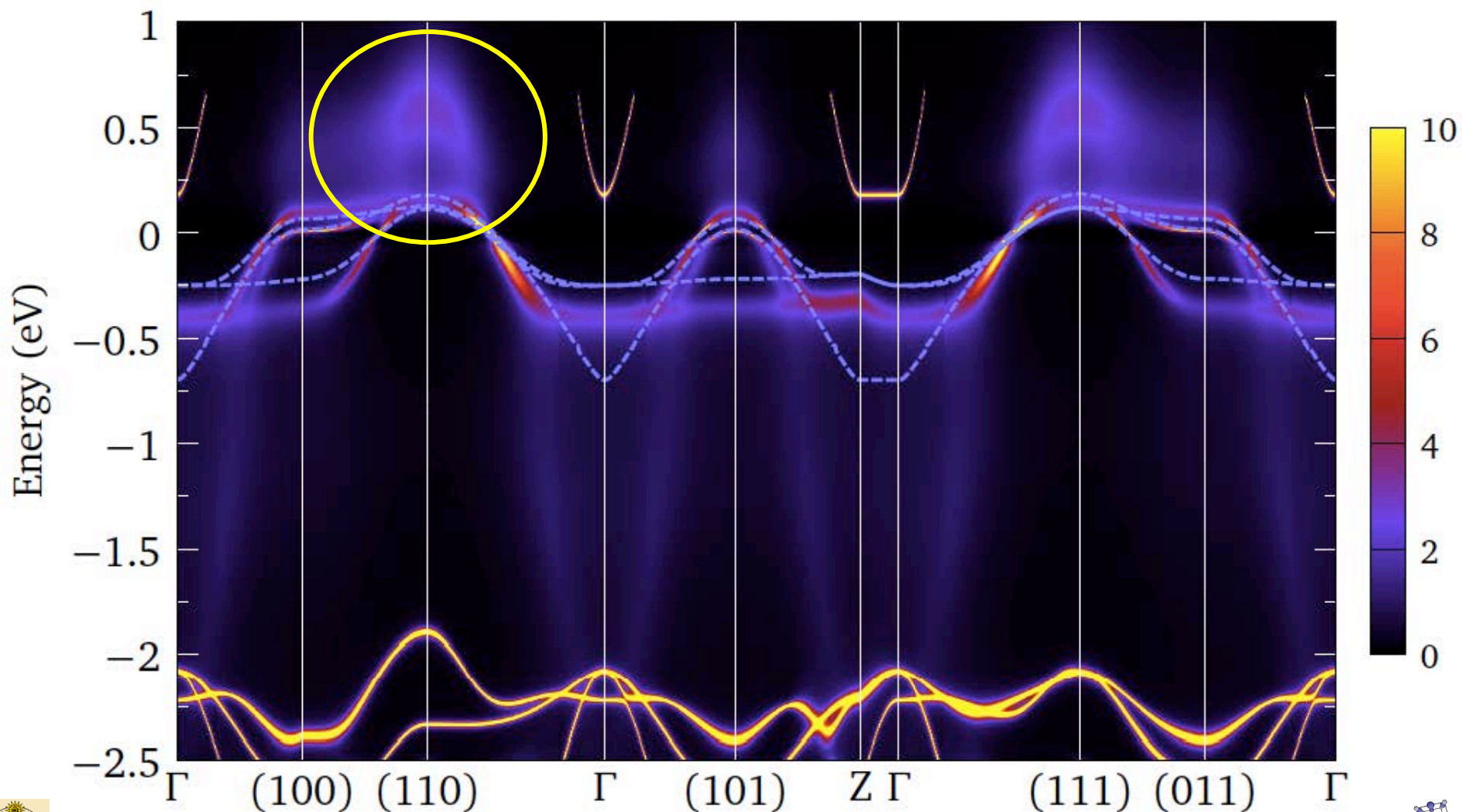
- Are broad, but with a scattering rate not exceeding $\sim \pi k_B T$, leading to clear peak in spectral function
- Do not obey Landau's T^2
- Have a dispersion which is **STRONGER** than the LDA one, in sharp contrast to the low-energy large effective mass in the Landau FL regime



Yet, outstanding puzzles about this compound remain...

- A 4d material → expect not very large U ($< 3\text{eV}$)
- Yet, strongly correlated : effective mass enhancement (vs. band/LDA value) as large as ~ 5
- Strong orbital dependence
- Low Fermi-liquid coherence scale:
 T^2 law obeyed only below $\sim 30\text{K}$
- Complex crossover in resistivity, from FL at low- T all the way to 'bad metal' (above Mott Ioffe Regel) at hi- T

‘Resilient’ quasiparticles: what is their dispersion ?
Predictions for momentum-resolved spectroscopies on the ‘dark side’ of the Fermi surface



Sr_2RuO_4 : A strongly interacting Fermi liquid

Universal scaling of the optical momentum relaxation rate:

$$1/\tau = A\{ (\hbar\omega)^2 + (2\pi k_B T)^2 \}$$

Fermi liquid and resilient quasiparticles:
excellent agreement with the DMFT predictions

Publications related to this presentation

Berthod, Mravlje, Deng, Žitko, vdMarel, Georges,
PRB 87, 115109 (2013)

*Mirzaei, Stricker, Hancock, Berthod, Georges, vHeumen, Chan, Zhao, Li,
Greven, Barišić, vdMarel,*
PNAS 110, 5774 (2013)

Stricker, Mravlje, Berthod, Fittipaldi, Vecchione, Georges, vdMarel,
PRL 113, 087404 (2014)

**SCSR2014 Adriatico Guesthouse, Trieste,
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The 11th International Conference on
Materials & Mechanisms of Superconductivity
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