

Optics Modeling and Simulation at APS —Hybrid method combining ray tracing and wavefront propagation

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Advanced Photon Source

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Outline

- Motivation
- Hybrid method
 - Combining ray tracing and wavefront propagation
 - Including mirror figure error
- Beamline design
 - In Situ Nanoprobe (ISN) beamline at APS
- Summary

Motivation

- New light sources and upgrades with higher brightness, shorter pulse lengths, smaller emittance and partial or full coherence
- New experimental techniques: nano-scale imaging/ diffraction/ spectroscopy, ultrafast/time resolved experiments, coherent diffraction imaging.

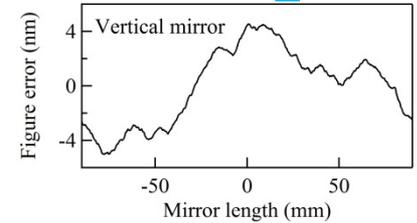
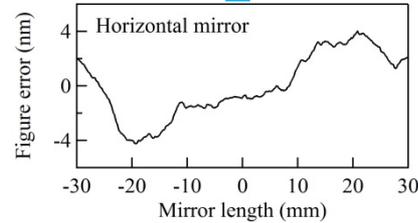
Optics simulation and modeling

- Geometrical ray tracing, e.g., SHADOW
 - Total intensity, beam size, mirror figure errors, reflectivity
 - Fast, robust, parameter optimization
- Wavefront propagation
 - Fourier optics, e.g., SRW
 - Stationary phase, e.g., PHASE
 - Field amplitude and phase, diffraction effect and beam coherence
 - Partial coherent source: multi-electron simulation

Combining ray tracing and wavefront propagation

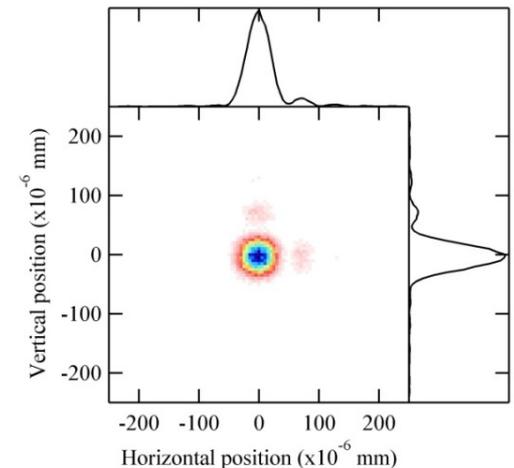
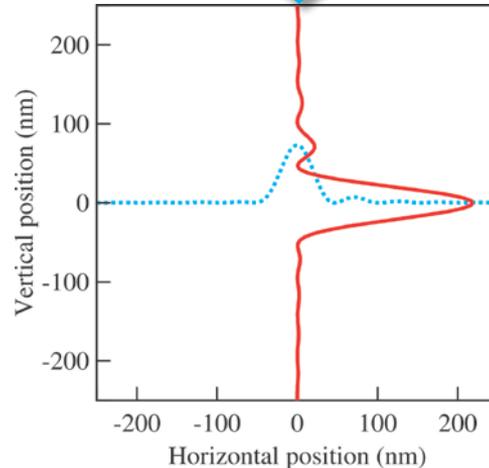
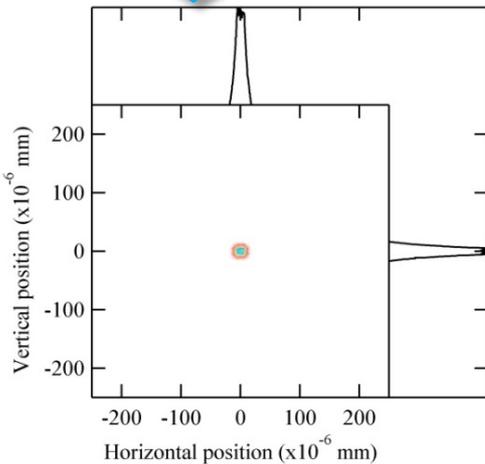
$$\text{Plane wave} \times \exp \left[-ik \left(\frac{x^2}{2f_x} + \frac{z^2}{2f_z} \right) \right] \times \exp[-i2k \sin \theta_x \cdot \text{Height}(x)] \times \exp[-i2k \sin \theta_z \cdot \text{Height}(z)]$$

Ideal lens with focal lengths of f_x and f_z

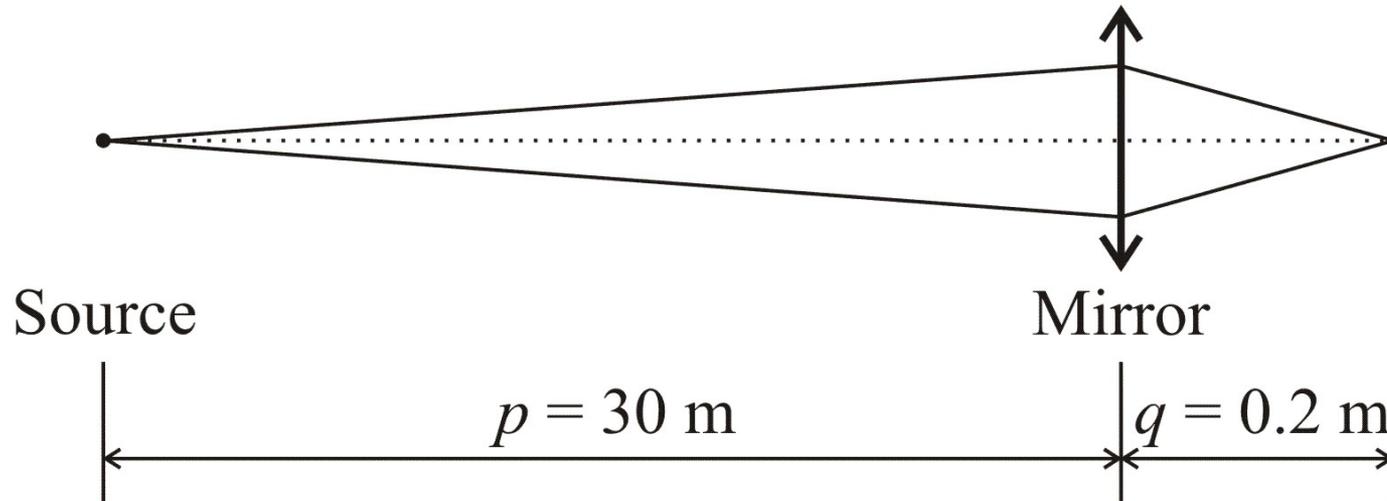


Ray tracing of the beamline

$$E(x, z) \rightarrow \boxed{\text{FFT}} \xrightarrow{\mathcal{F}(u,v)} \times \exp \left[-\frac{i2\pi^2}{k} (u^2 + v^2)y \right] \xrightarrow{\mathcal{F}'(u,v)} \boxed{\text{Inverse FFT}} \rightarrow E(x', z')$$



Testing case

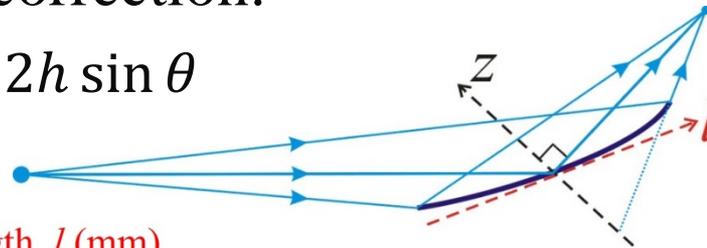


- Source:
 - $\sigma = 2 \text{ } \mu\text{m}$
 - $\sigma' = 30 \text{ } \mu\text{rad}$
 - $E = 10 \text{ keV}$
- Elliptical cylinder mirror
 - Mirror length $l = 200 \text{ mm}$
 - Grazing angle at mirror center: $\theta_0 = 2.5 \text{ mrad}$
 - Demagnification: 150:1

Angle correction and intensity scaling

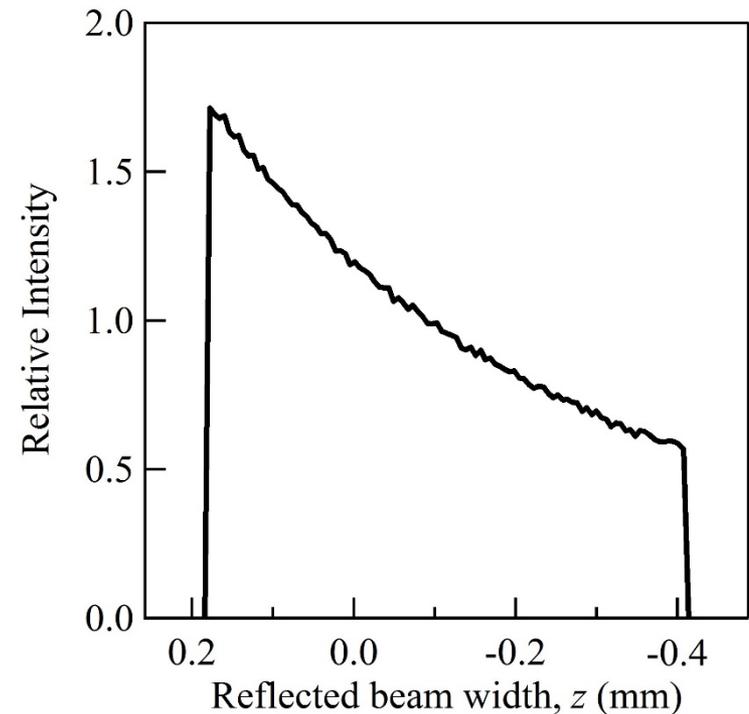
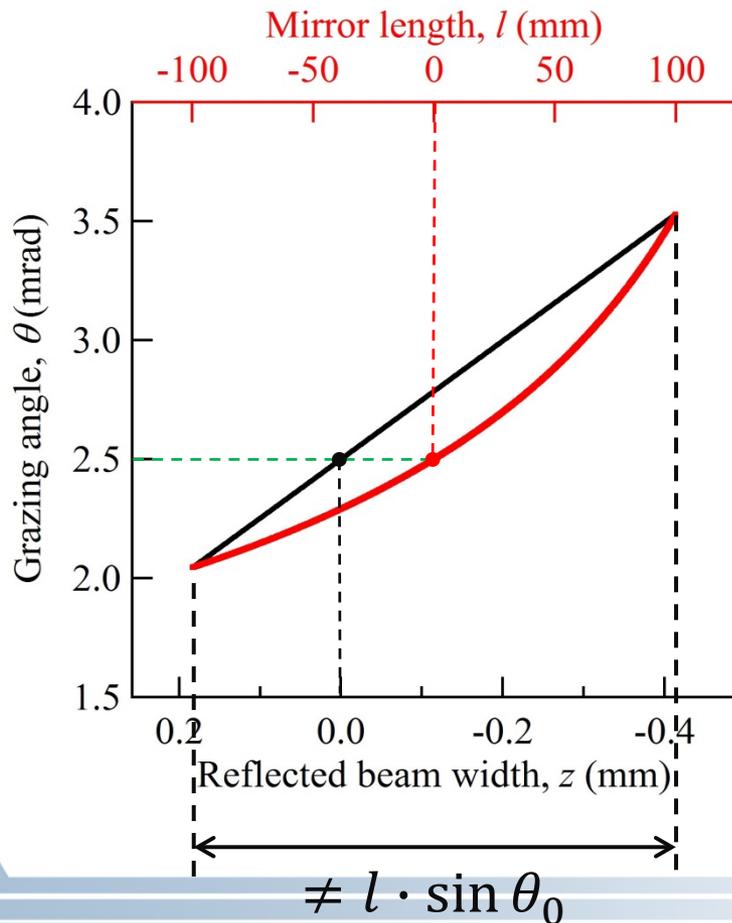
- Grazing angle correction:

$$\Delta\phi = (2\pi/\lambda) \cdot 2h \sin \theta$$



- Intensity scaling

$$E \propto \sqrt{I}$$



Angle correction and intensity scaling: effects on image

- No slope error
- Ray tracing + diffraction
- Ray tracing + diffraction + intensity scaling

- Slope error: $0.3 \mu\text{rad}$
- Ray tracing + diffraction
 - Ray tracing + diffraction + angle correction
 - Ray tracing + diffraction + intensity scaling
 - Ray tracing + diffraction + angle correction + intensity scaling

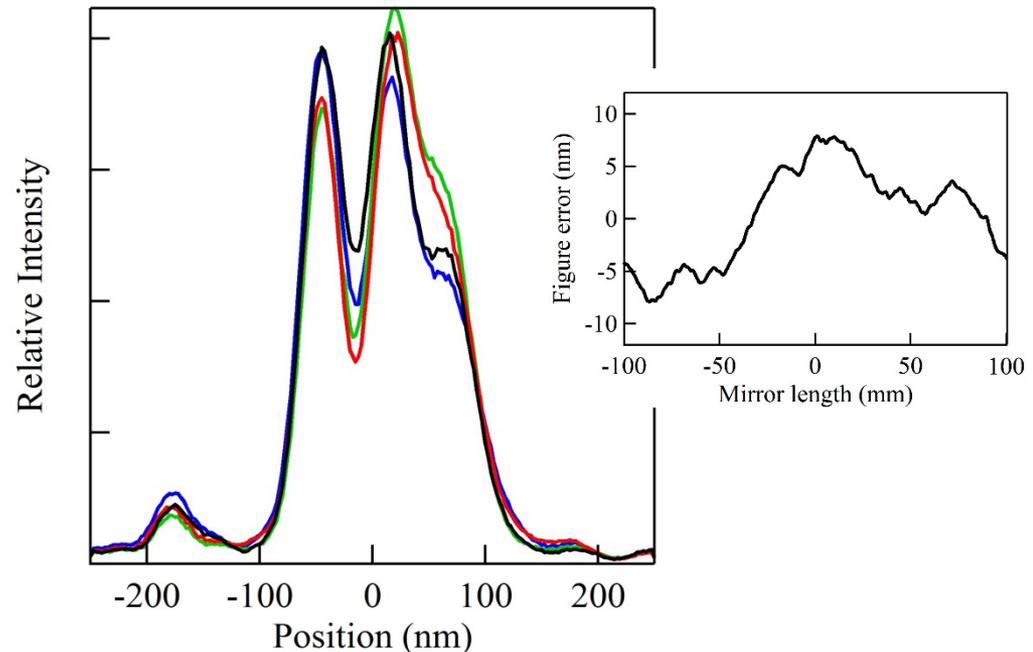
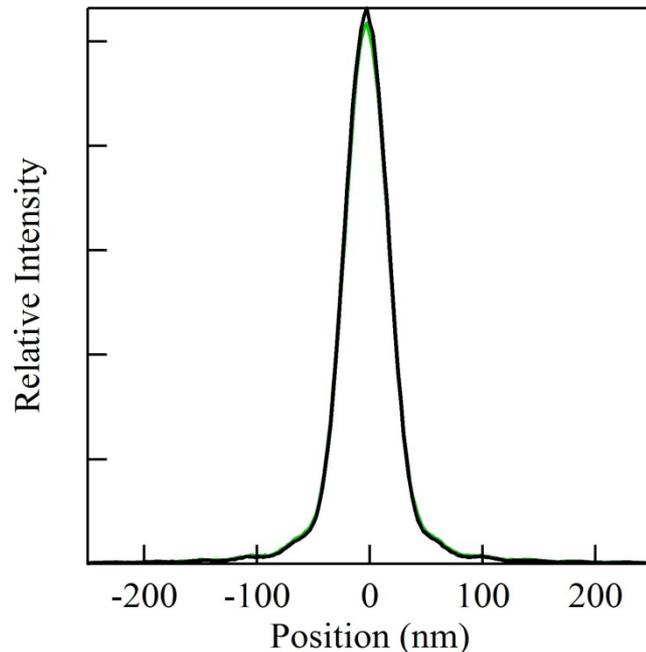


Figure error frequencies - Grating effect

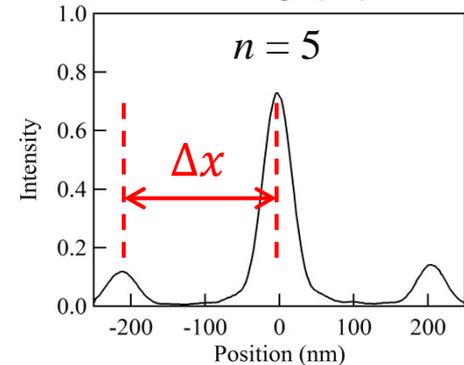
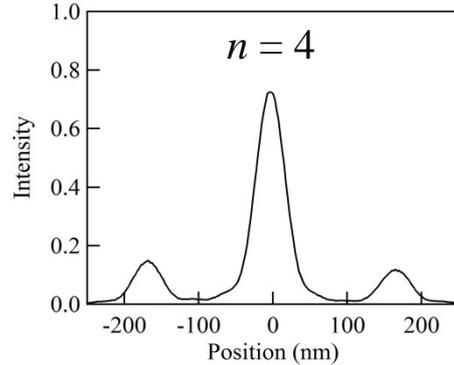
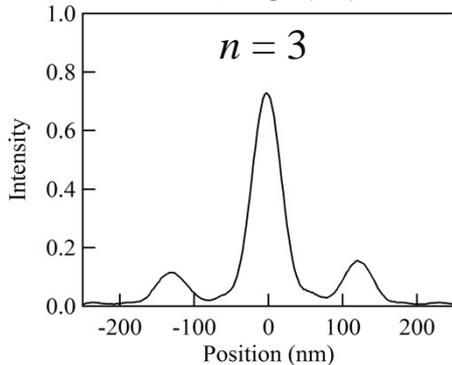
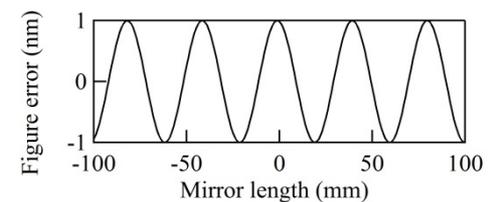
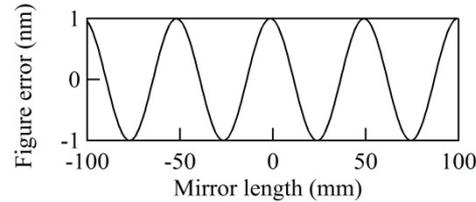
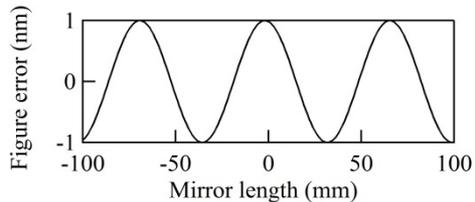
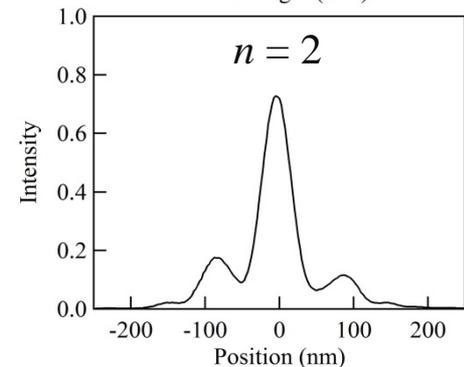
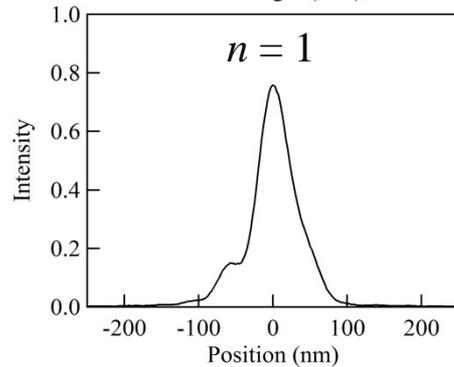
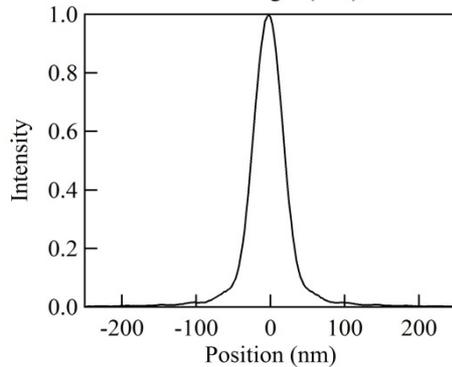
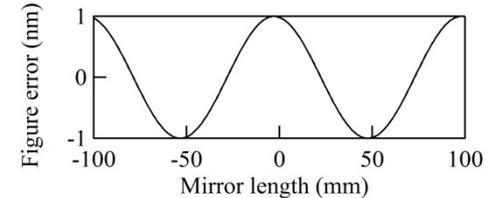
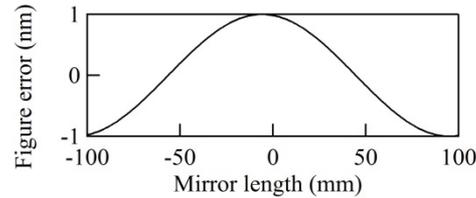
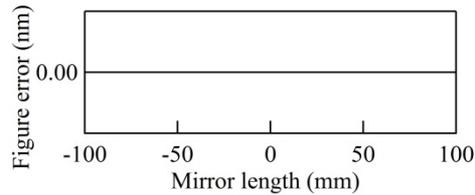
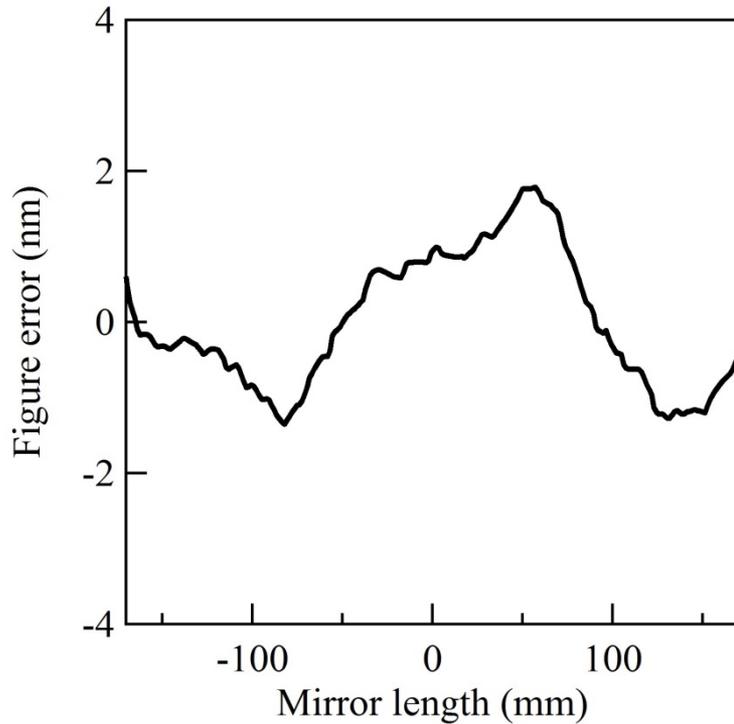


Figure error frequencies - PSD



LCLS mirror

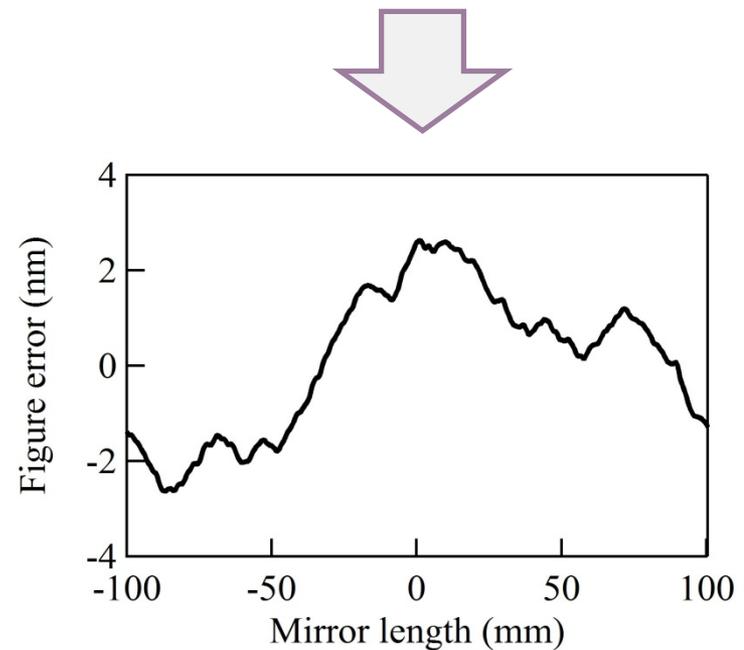
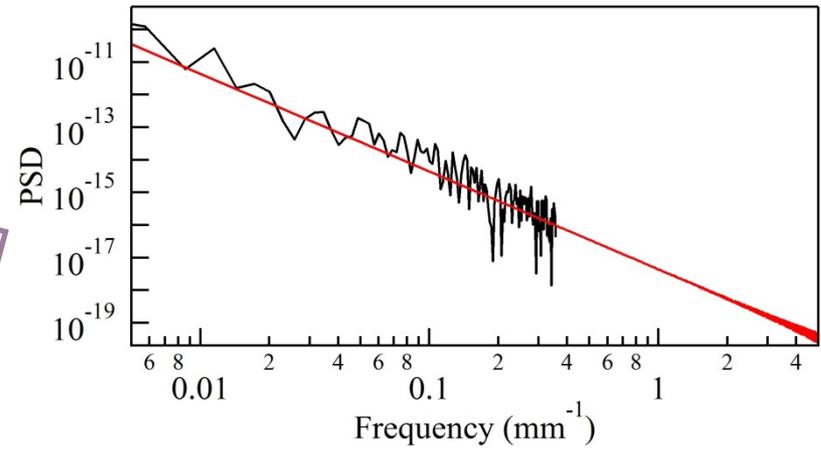
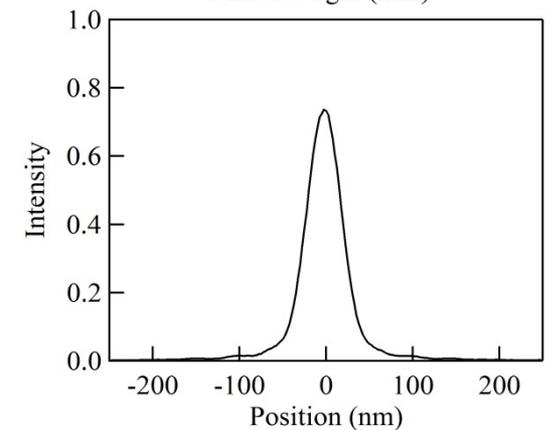
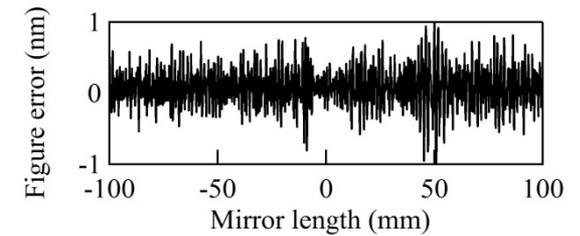
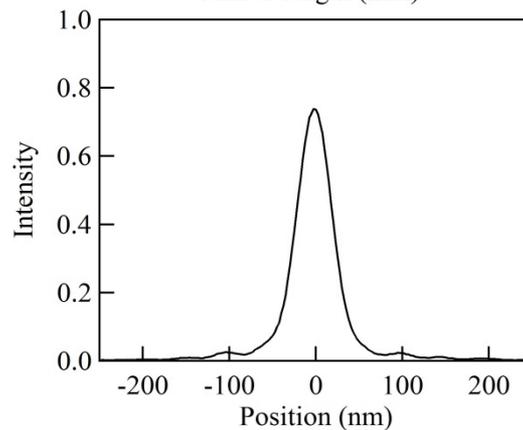
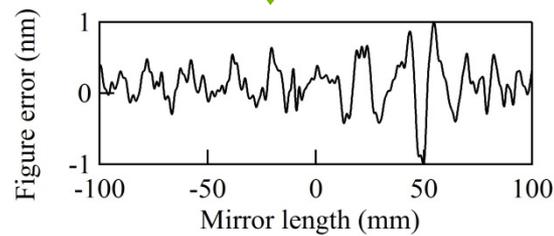
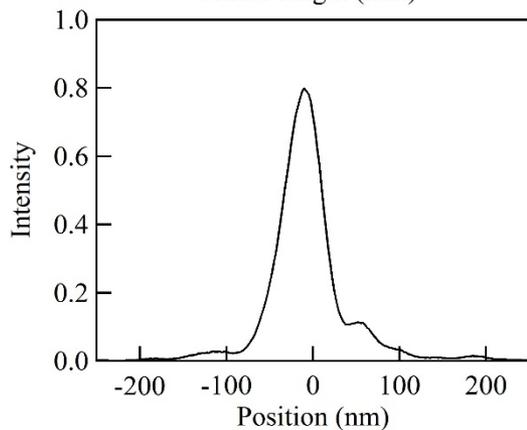
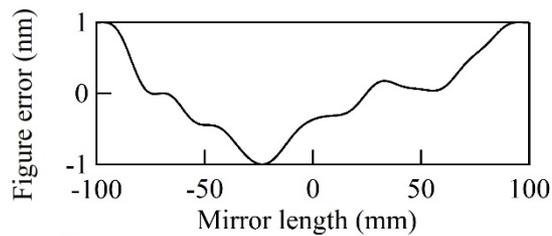
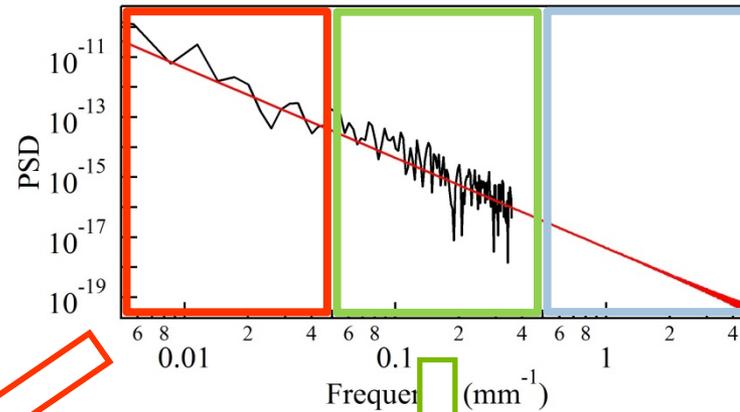


Figure error frequencies - PSD



Comparison with pure ray tracing

Diffraction limited

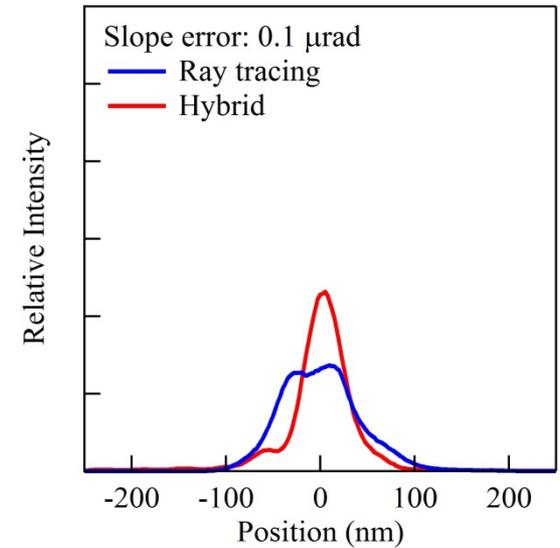
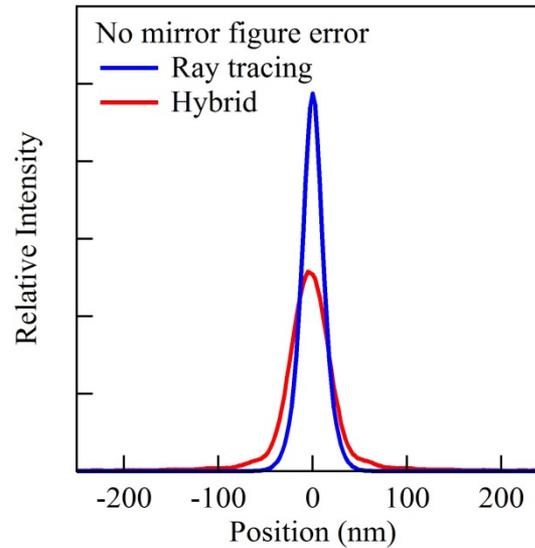
$$\sigma = 2 \mu\text{m}$$

$$\sigma' = 30 \mu\text{rad}$$

$$p = 30 \text{ m}$$

$$q = 0.2 \text{ m}$$

$$l = 0.2 \text{ m}$$



Not diffraction limited

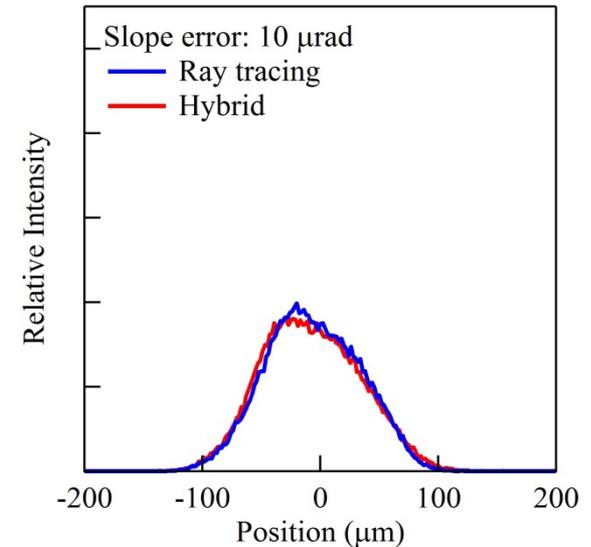
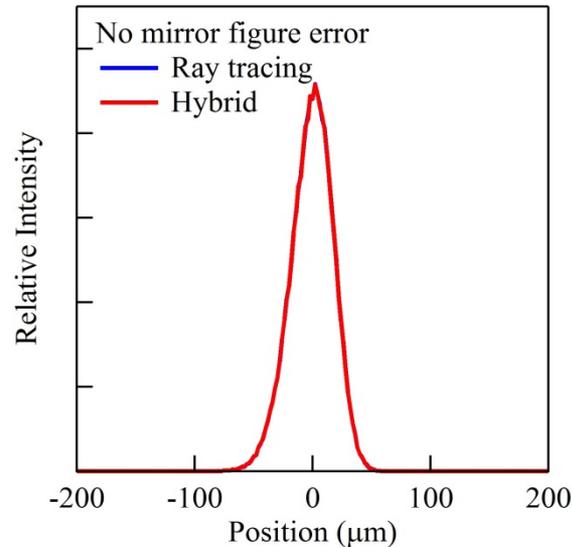
$$\sigma = 270 \mu\text{m}$$

$$\sigma' = 12 \mu\text{rad}$$

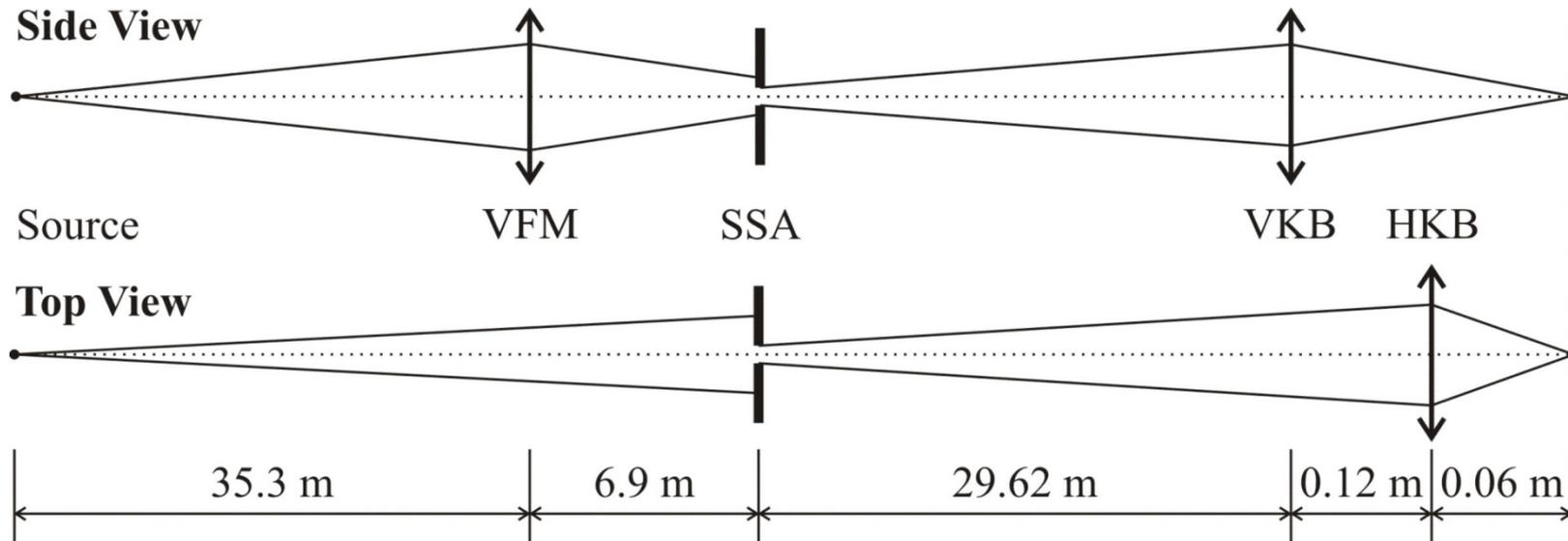
$$p = 30 \text{ m}$$

$$q = 2 \text{ m}$$

$$l = 1 \text{ m}$$



In Situ Nanoprobe beamline



Photon (10 keV)	Electron	Total
$\sigma_r = 3.86 \mu\text{m}$	$\sigma_x = 274.3 \mu\text{m}$	$\sigma_x = 274.3 \mu\text{m}$
	$\sigma_y = 10.3 \mu\text{m}$	$\sigma_y = 11.0 \mu\text{m}$
$\sigma_\xi = 5.11 \mu\text{rad}$	$\sigma'_x = 11.27 \mu\text{rad}$	$\sigma'_x = 12.4 \mu\text{rad}$
	$\sigma'_y = 3.58 \mu\text{rad}$	$\sigma'_y = 6.24 \mu\text{rad}$

Source: undulator A, 3.3 cm, 72 periods, $K = 0.906$, $B = 0.294 \text{ T}$

VFM: 400 mm long, 2.5 mrad grazing angle

SSA: $11 \times 4 \mu\text{m}^2$ (h \times v)

VKB: 180 mm long, 2.5 mrad grazing angle

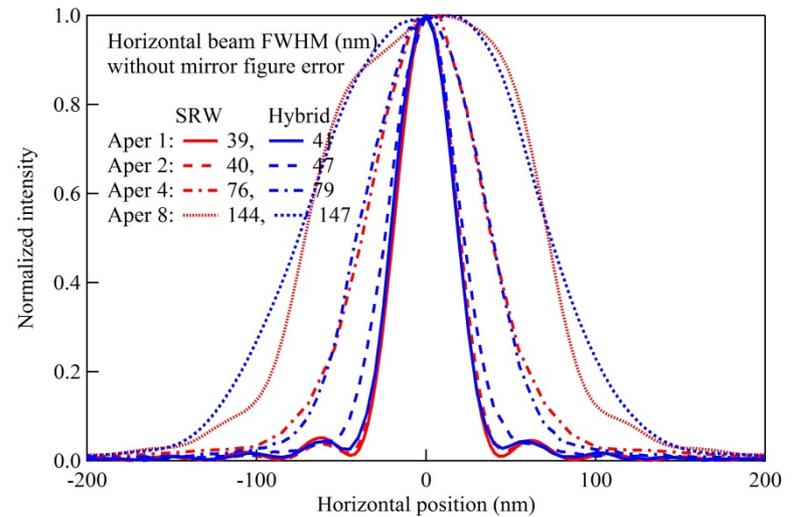
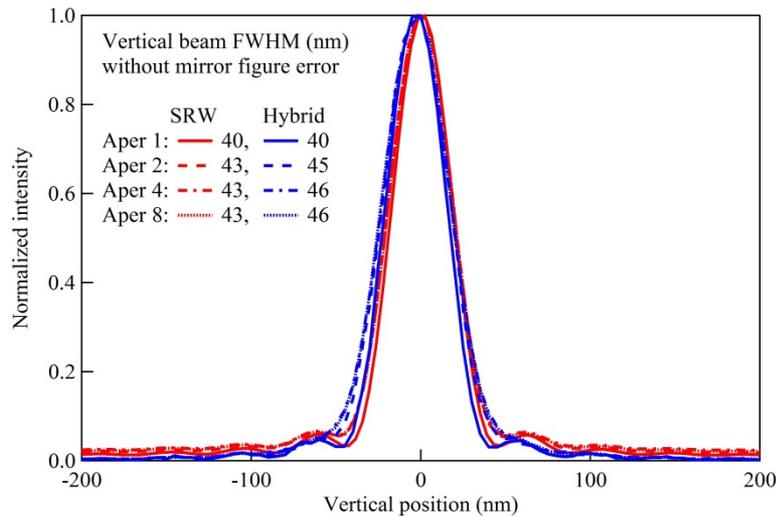
HKB: 60 mm long, 2.5 mrad grazing angle

Comparison with SRW (multi-electron)

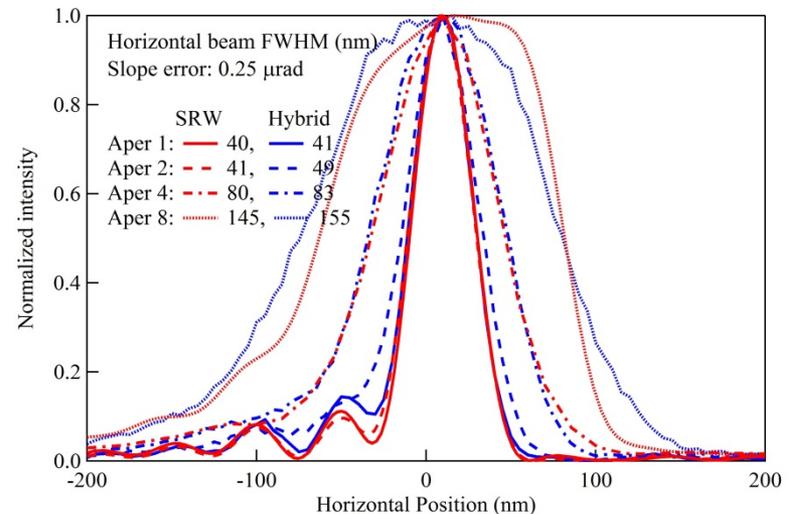
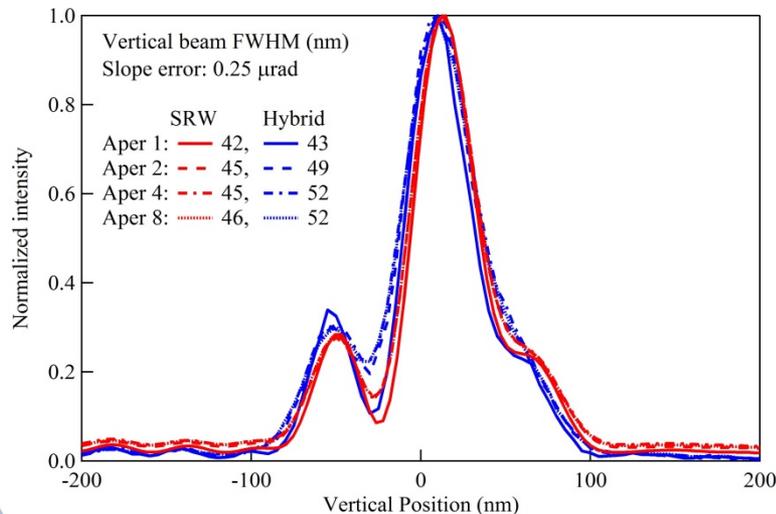
Without figure error

Calculation time: SRW: 32 core × 5 hours

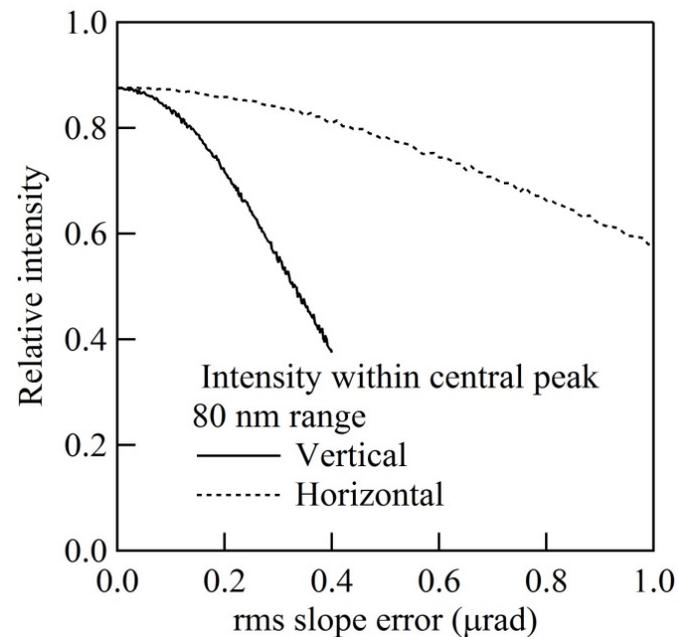
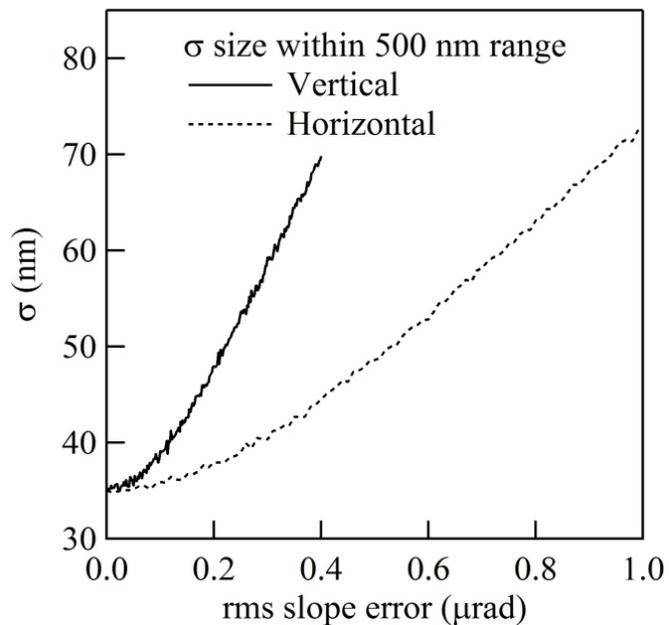
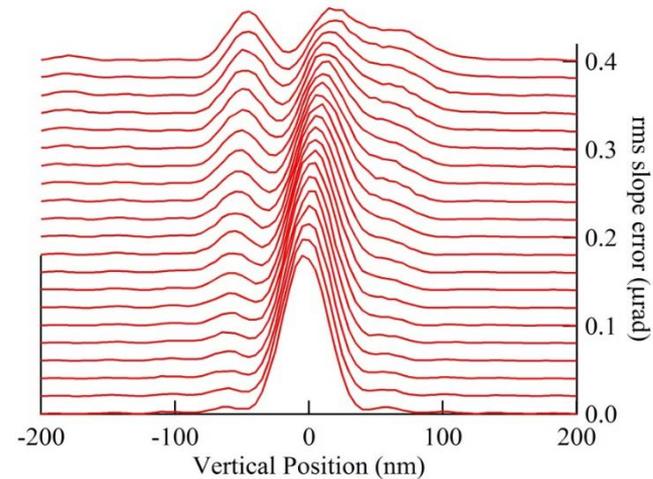
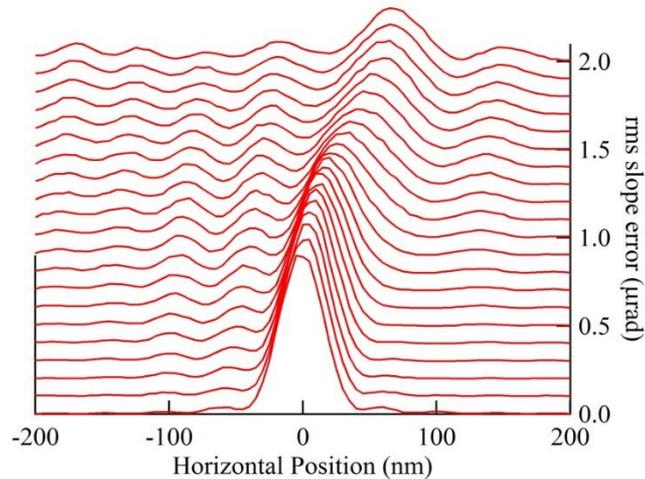
Hybrid: 1 core × 5 minutes



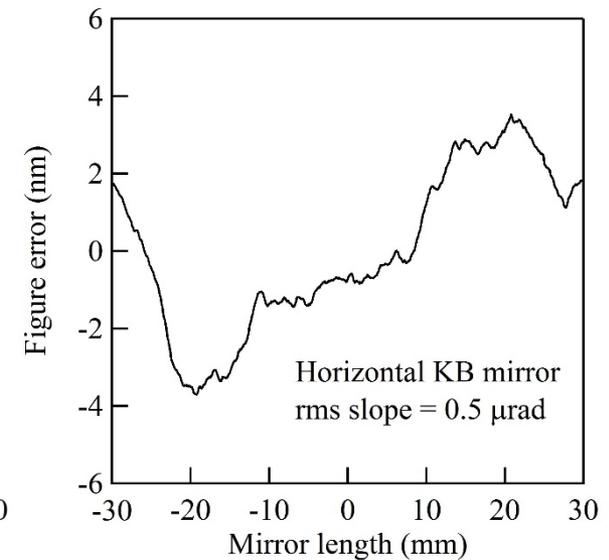
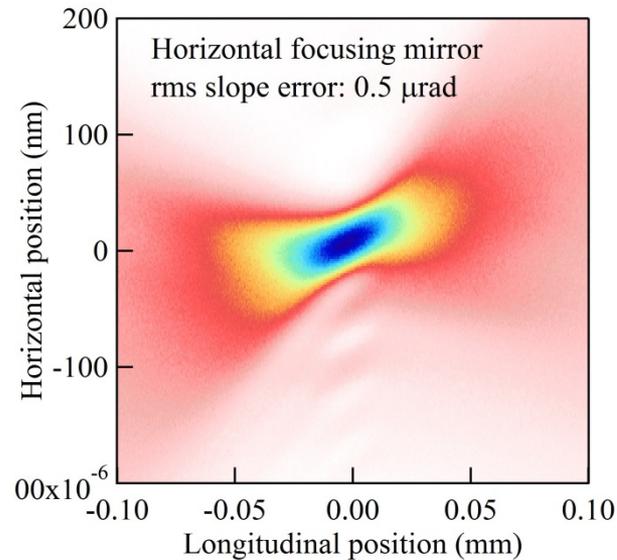
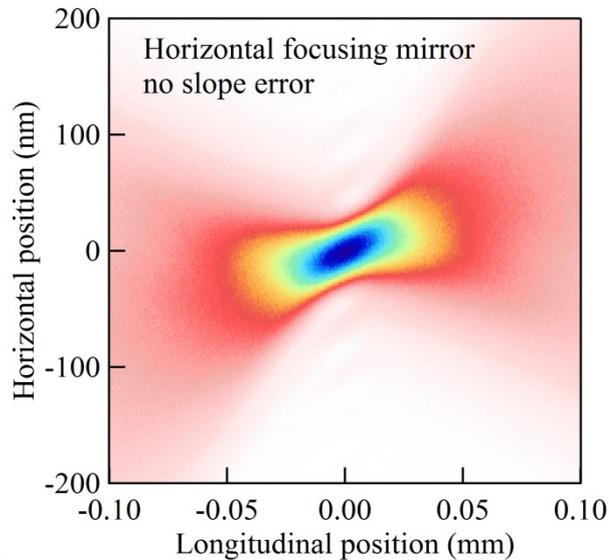
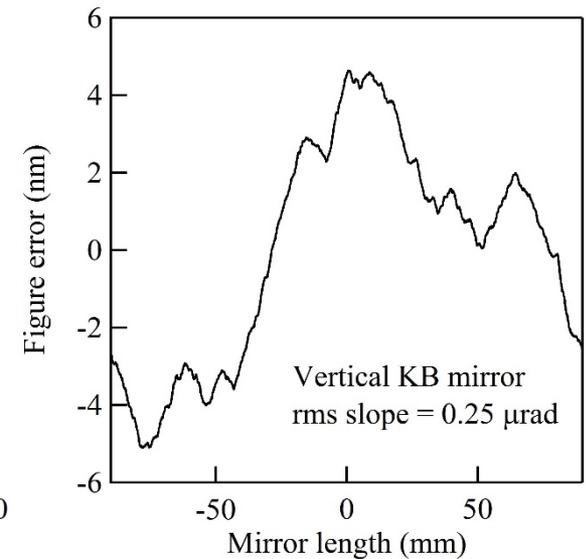
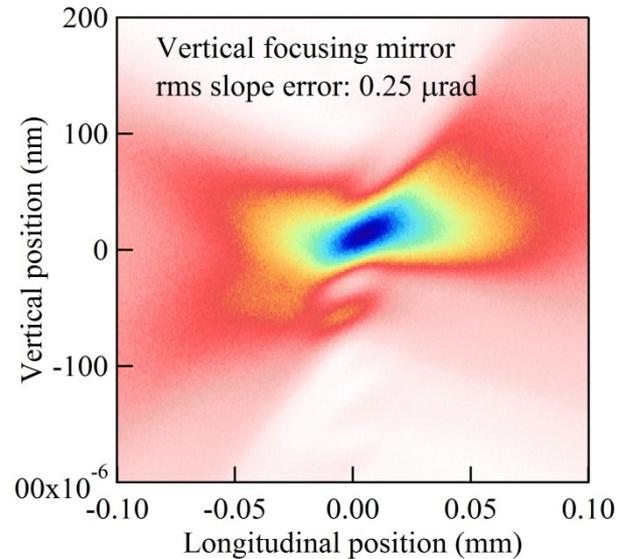
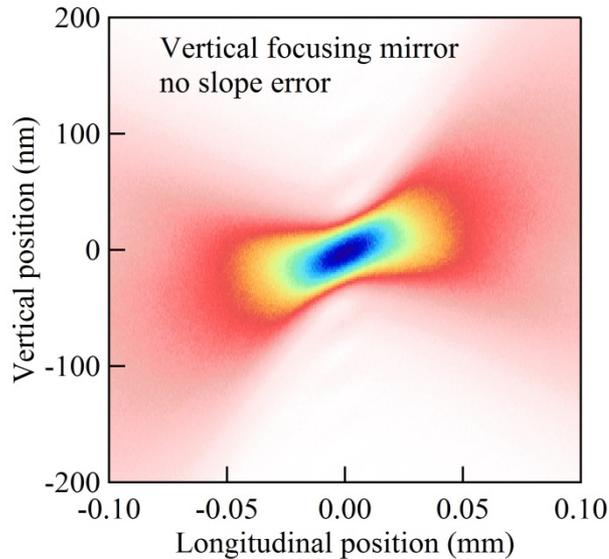
With figure error



KB mirror slope error studies



Beam profiles along longitudinal direction



Summary

- ✓ The hybrid method combining ray tracing and wavefront propagation is demonstrated and compared with existing codes. It will be implemented in SHADOW.
- ✓ The effects of mirror figure error are studied. A bank of real metrology data will greatly benefit the community.
 - Full 2-D simulation is needed for certain cases (toroid mirror).
 - Coherence properties are the next focus.

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