

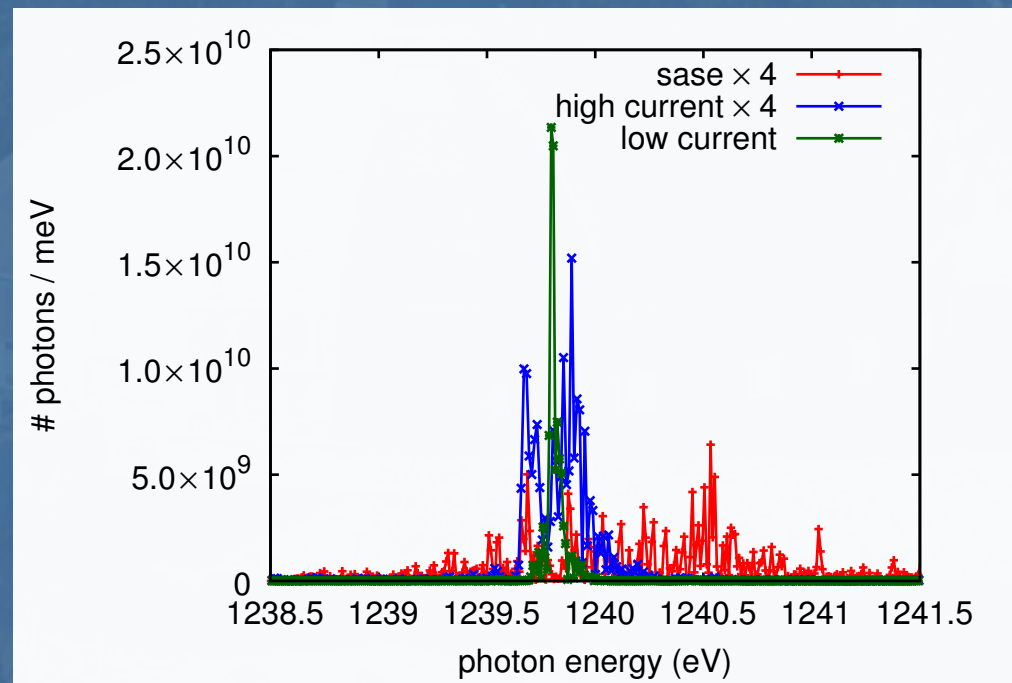
# Coherence Requirements for Various Seeding Schemes

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# Coherence is a major goal of seeding

## Laser seed phase errors

- multiplied by harmonic jump
- straightforward and unavoidable, not considered here
- small effect from laser seed power profile

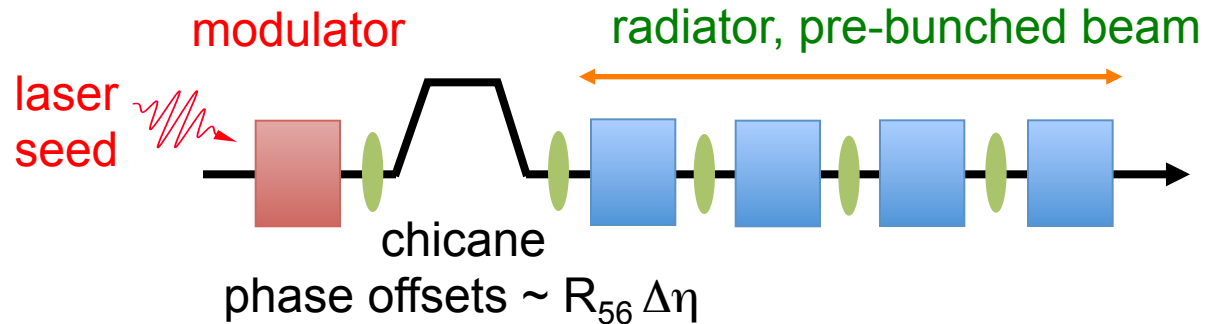
## Shot noise

- required seed power grows with square of harmonic

## Electron beam slice variations (scale $> L_{\text{coop}}$ )

- focus on slice energy
- peak current and emittance weaker

# Start with HGHG



Phase variations from energy profile dominated by chicane

$$\Delta\theta = \frac{2\pi}{\lambda_r} R_{56} \Delta\eta$$

$\Delta\eta =$  rel slice energy offset

$$\Delta z = R_{56} \Delta\eta$$

avoids confusion when  
wavelength changes

(arbitrary sign choices, 'normal' chicane  $R_{56} > 0$ )

# Phase Errors Still Grow after Chicane

initial bunched beam  $\rightarrow$  radiation phase

a good fit is

$$\Delta\theta \simeq \begin{cases} \frac{2\pi}{\lambda_u} L_u \Delta\eta, & L_u < 4.5L_g \\ 1.2 \frac{2\pi}{\lambda_u} \left( L_u - \frac{3}{4}L_g \right) \Delta\eta, & L_u > 4.5L_g. \end{cases}$$

by analogy, define as

$$\Delta z \equiv R_{\text{rad}}^{\text{FEL}} \Delta\eta$$

shorthand: “R value” for radiator with pre-bunching

# R<sup>FEL</sup> for prebunched beams

$$R_{\text{rad}}^{\text{FEL}} \simeq \begin{cases} \frac{\lambda_r}{\lambda_u} L_u, & L_u < 4.5L_g \\ 1.2 \frac{\lambda_r}{\lambda_u} \left( L_u - \frac{3}{4}L_g \right), & L_u > 4.5L_g \end{cases}$$

levels off at  $\sim 1.2 L_{\text{sat}} \lambda_r / \lambda_u$  after saturation

R<sub>56</sub> for undulators is  $L_u (1 + a_u^2) / \gamma^2 = 2L_u \lambda_r / \lambda_u$

- low gain, R<sup>FEL</sup> is half of R<sub>56</sub> from beamline
- L<sub>u</sub> is magnetic length
  - more accurate, use  $L_u + L_{\text{drift}} / (1 + a_u^2)$

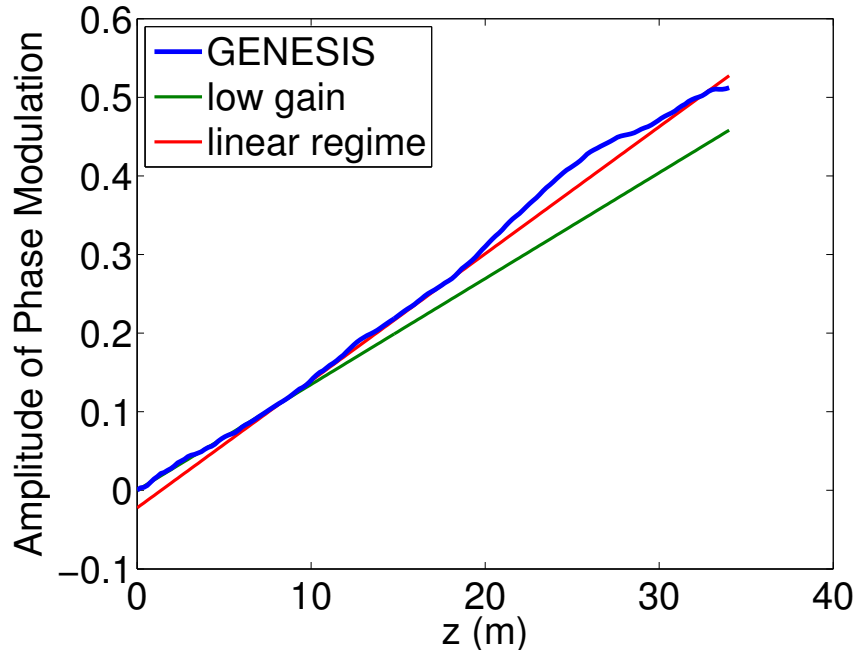
same result for modulator

- initial radiation field → modulation phase

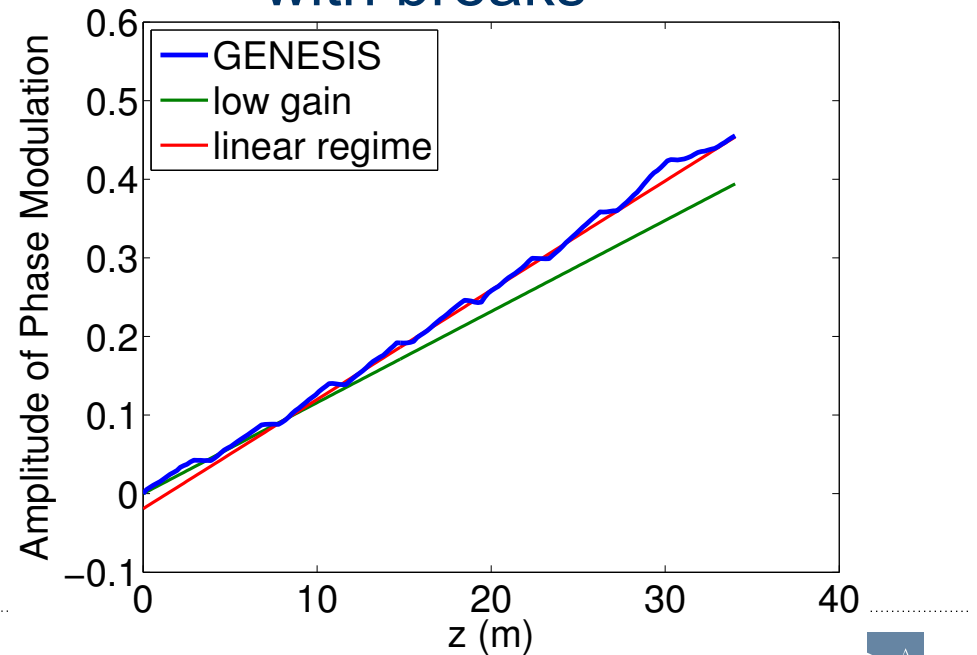
# Prebunched beam: fit to simulations

- e-beam: 2.4 GeV, 0.6 micron, 600 A, 250 keV spread
  - und: 20 mm pd, 3 m sections, tuned for 1 nm output
- 100 keV energy modulation is applied: track phases

uniform



with breaks



# Close to 1D FEL theory

3 modes, only 1 growing

growth rates up to linear in  $\Delta\eta$ :

$$\Gamma_+ = \frac{1}{2L_{1D}} \left( 1 + \frac{i}{\sqrt{3}} \right) - \frac{4}{3} i k_u \Delta\eta$$

$$\Gamma_0 = \frac{1}{2L_{1D}} \left( 1 + \frac{i}{\sqrt{3}} \right) - \frac{4}{3} i k_u \Delta\eta$$

$$\Gamma_- = \frac{1}{2L_{1D}} \left( -\frac{2i}{\sqrt{3}} \right) - \frac{4}{3} i k_u \Delta\eta$$

initial mix for bunching with no modulation or field

differences from numerical fit:

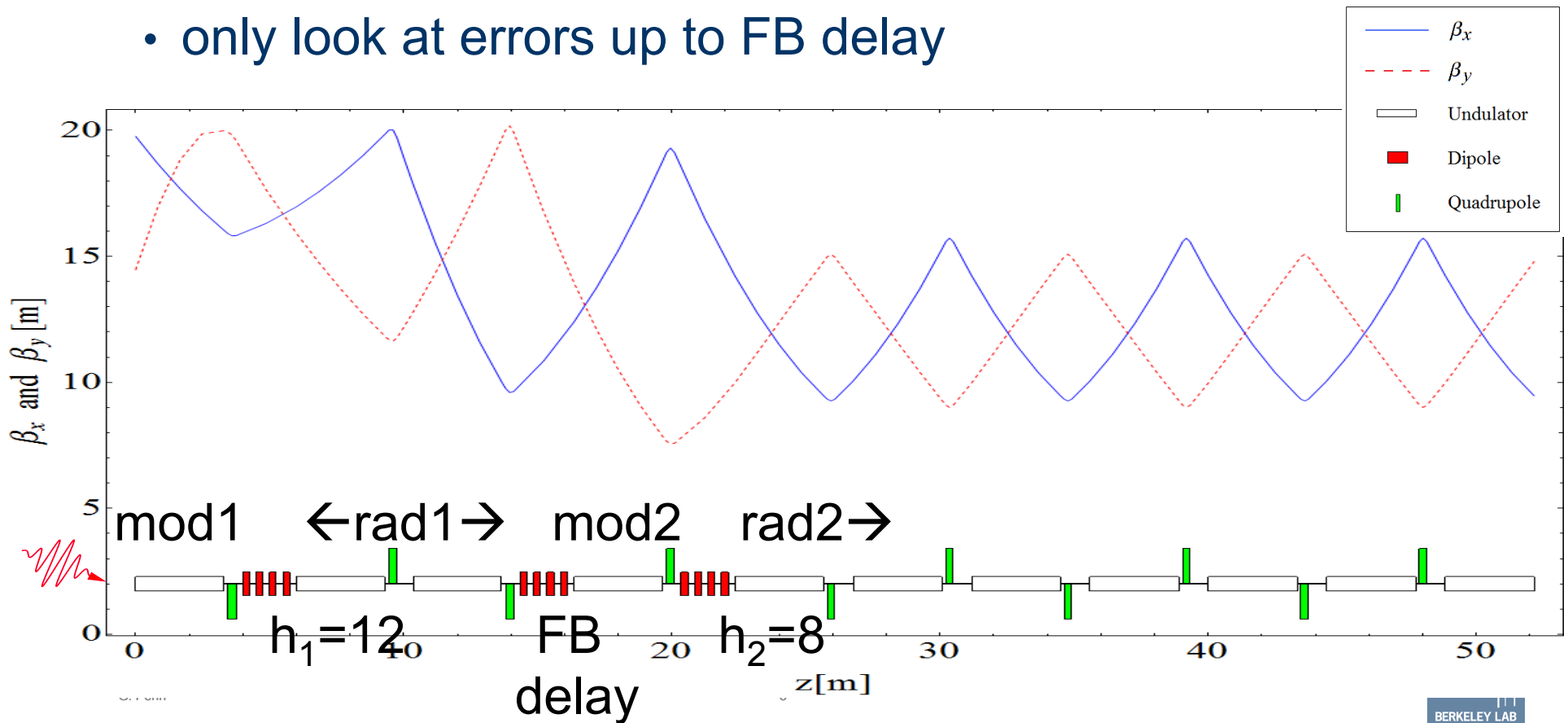
- replace  $L_g$  with  $L_{1D}$ , and 1.2 factor with  $2 \times 2/3$

2/3 because bunch & modulation affected by dispersion,  
but not radiation; 4/3  $\rightarrow$  1.2 due to diffraction?

# 2-stage HGHG example

2.4 GeV, 200 nm seed laser, 150 keV  $\sigma_E$ , **fresh-bunch**

- offsets before and after fresh bunch uncorrelated
- only look at errors up to FB delay





# Sensitivity to energy offsets

Total effect:

$$R^{\text{FEL}} = R_{\text{mod}}^{\text{FEL}} + R_{56} + R_{\text{rad}}^{\text{FEL}}$$

$$26.5 \mu\text{m} = 9 \mu\text{m} + 16 \mu\text{m} + 1.5 \mu\text{m}$$

- first chicane usually largest term

$$R_{56} \approx \frac{\lambda_{\text{seed}}}{2\pi\eta_M}$$

$\eta_M$  = rel energy modulation,  
typically  $\leq \rho_{\text{FEL}}$

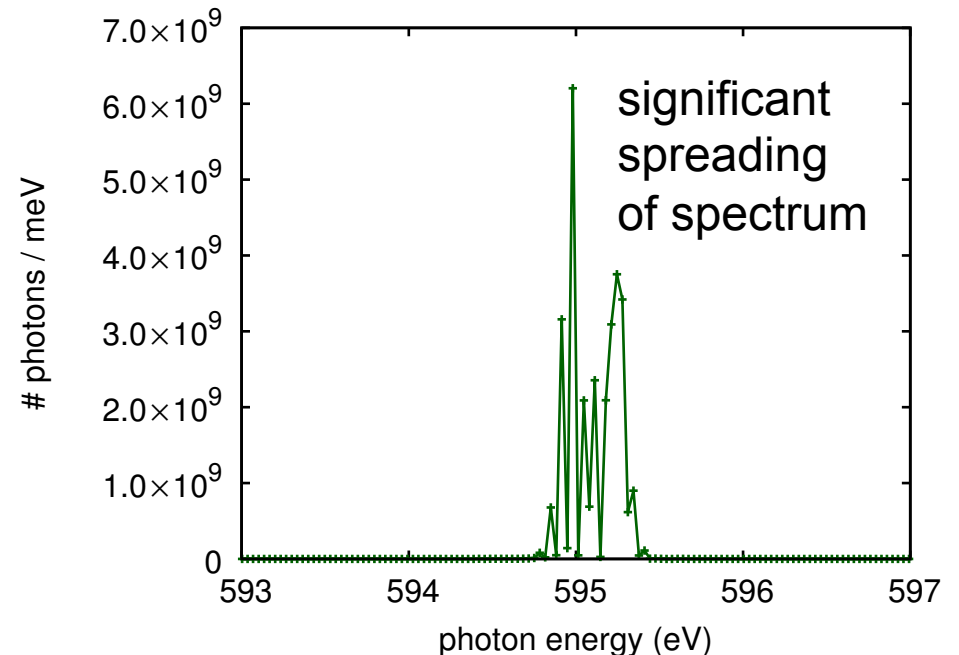
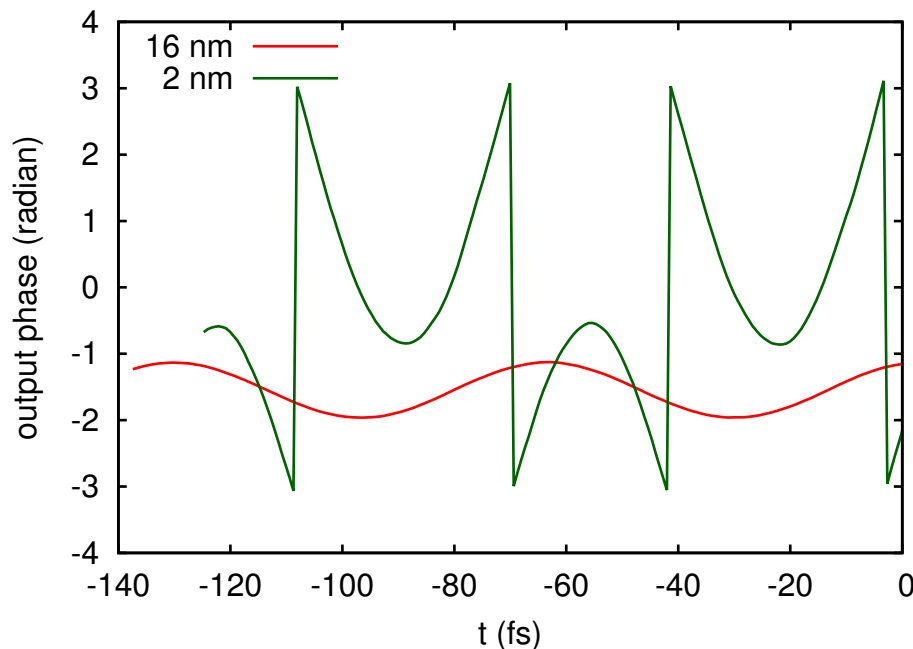
- energy modulation of 3.5 MeV yields  $R_{56}=16 \mu\text{m}$
- also some bunching in modulator

# Output Phase and Spectrum

100 keV offsets: 1.1 nm shifts in location of microbunch

1<sup>st</sup> stage (16 nm) and 2<sup>nd</sup> stage (2 nm)

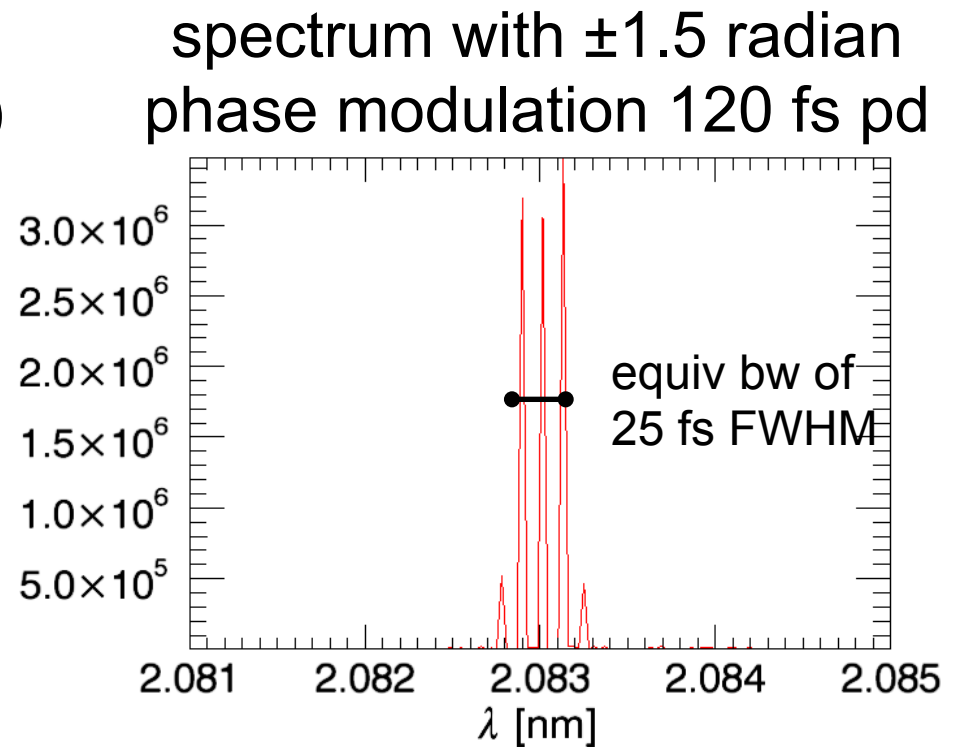
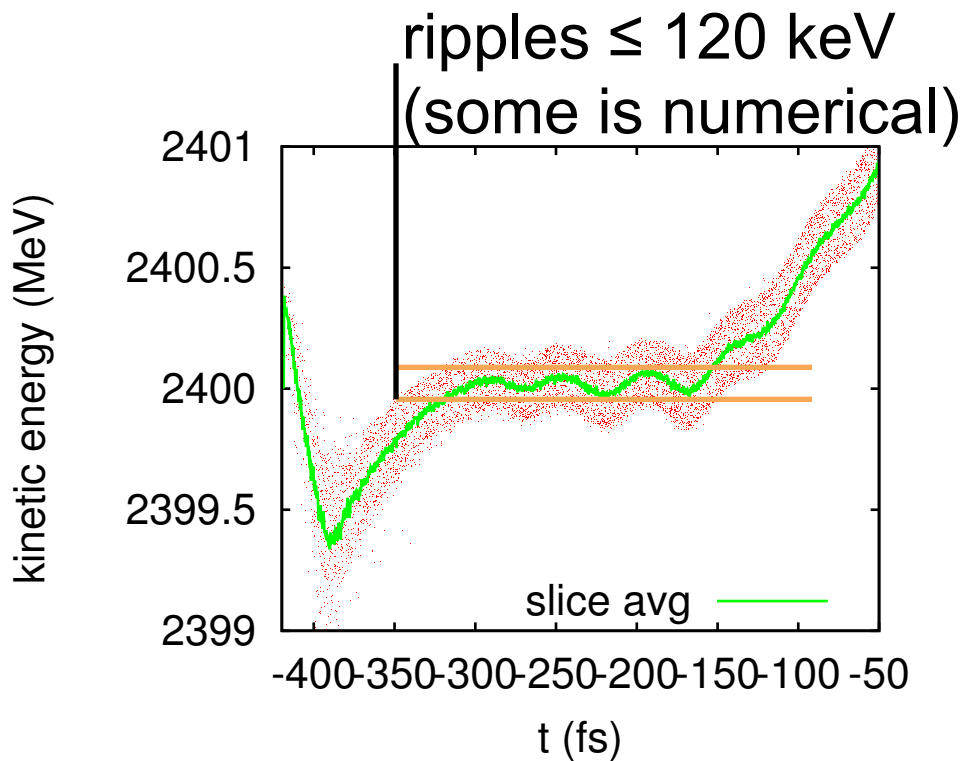
- at 2 nm > +/- 3 radian;  $R^{\text{FEL}} = 23 \mu\text{m}$



using avg phase; on-axis phase looks a little worse

# Simulated beam from RF gun

not an accurate estimate of microbunching



# How to get more tolerance to chirp?

More modulation, weaker chicane?

- modulator already contributes a lot
- self-bunching (no chicane) degrades performance

Negative  $R_{56}$  chicane?

- have to unwind bunching from modulator

$$-18 \mu\text{m} = 9 \mu\text{m} - 29 \mu\text{m} + 2 \mu\text{m}$$

- more complex, usually not tunable

either way, get less than 50% improvement

- needs further study

# Optical Klystron: new constraints

similar configuration, just no harmonic jump

- saturate sooner
  - V.N. Litvinenko, NIMA **304** (1991) 463
- low-power HHG seeds
  - M. Gullans *et al.*, Opt. Commun. **274** (2007) 167
- oscillators, ...
  - G. Dattoli *et al.*, J. Quan. Elec. 31 (1995) 1584

optimal bunching when  $kR_{56}\sigma_{\eta} \sim 1$

- but phase errors are  $kR_{56}\Delta_{\eta}$ , order unity when  $\Delta_{\eta} \sim \sigma_{\eta}$
- if only care about power, use *slice* energy spread
- if care about coherence, use *harmonic*  $\times \Delta_{\eta}$

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(typically,  $\Delta_{\eta} \sim$  projected energy spread)

# Self-seeding and $R^{\text{FEL}}$

only post-monochromator stage has an impact

- initial radiation  $\rightarrow$  final radiation phase
- same analysis, different dependence

$$R_{\text{SS}}^{\text{FEL}} \simeq \begin{cases} 0, & L_u < 1.5L_g \\ 1.2 \frac{\lambda_r}{\lambda_u} \left( L_u - \frac{3}{2}L_g \right), & L_u > 1.5L_g. \end{cases}$$

also close to 1D theory:

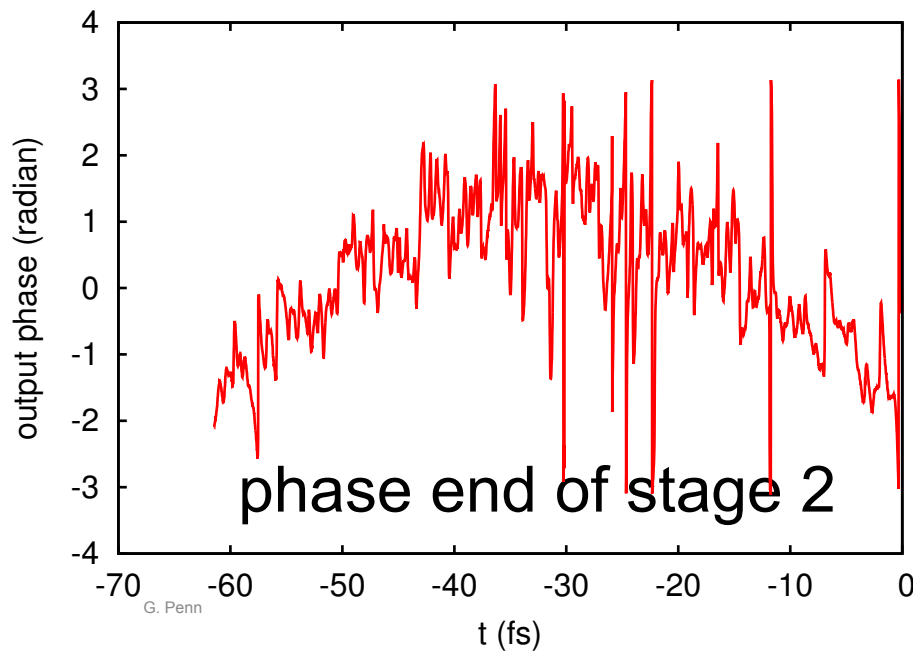
- low gain, no change in phase by definition of low gain
- linear regime would have 4/3 instead of 1.2

# LCLS HXRSS self-seeding

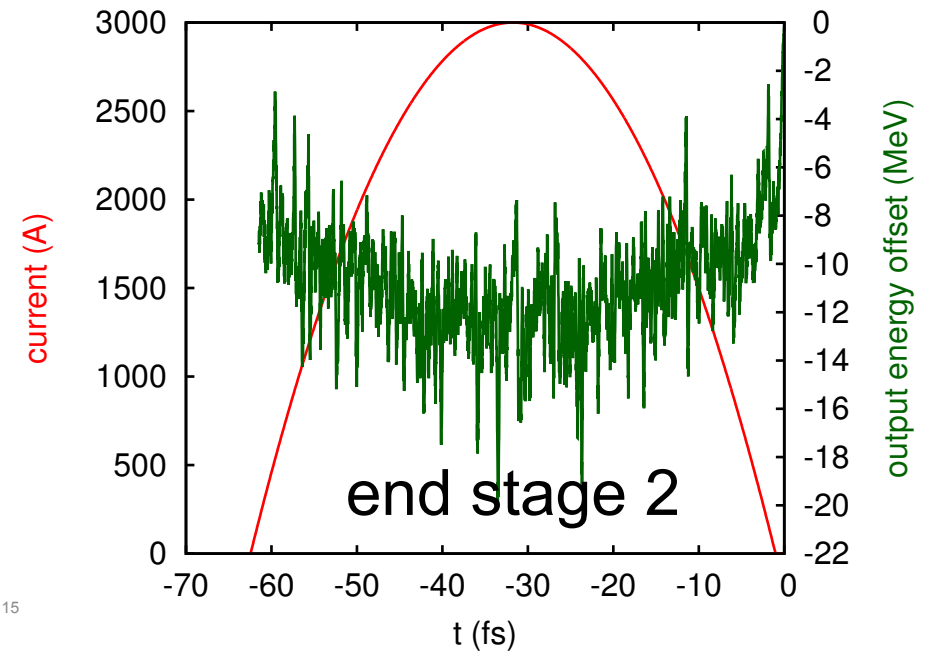
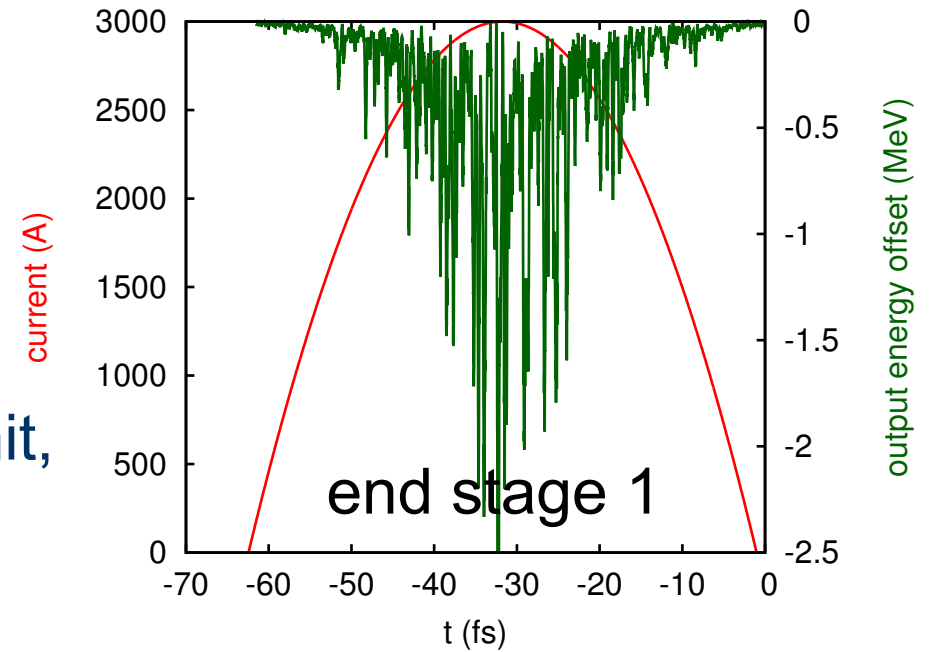
electron beam:

- 13 GeV, 3 kA, 0.4  $\mu\text{m}$  emit, parabolic profile

radiate at 0.15 nm



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# EEHG has intriguing result

In echo scheme, mixing two waves:

- output  $k_x = pk_2 - mk_1$                        $p, m$  integers;  $k = 2\pi/\lambda$
- smaller phase errors in bunching than HGHG\*

$$\Delta\theta = (k_x R_2 - mk_1 R_1) \Delta\eta$$

- so

$$R_{\text{echo}}^{\text{FEL}} = R_2 - mR_1 \lambda_x / \lambda_1$$

- two terms can partly cancel, but bunching

$$b \propto J_m [(k_x R_2 - mk_1 R_1) \eta_{M1}]$$

- if  $\arg=0$ , no bunching

$\eta_{M1}$ is 1st relative energy modulation
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# EEHG less sensitive to energy offsets

usually  $m=1$ , Bessel function yields soft optimum

$$|k_x R_2 - k_1 R_1| \simeq 1.8/\eta_{M1}$$

very good scaling, almost cancels

- ratio of terms is  $1.8 (\eta_{M2}/\eta_{M1}) (\lambda_2/\lambda_x)$
- $R^{\text{FEL}}$  goes like output wavelength, not seed wavelength

$$R_{\text{echo}}^{\text{FEL}} = R_2 - m R_1 \lambda_x / \lambda_1$$

# Easy control over sign of $R^{\text{FEL}}$

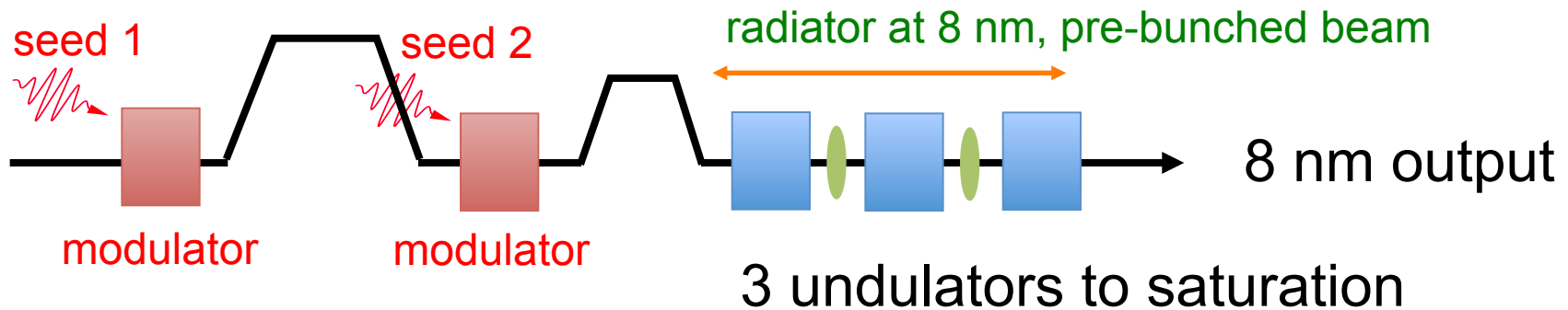
useful feature, EEHG has two optimal settings for  $R_1$

- for given  $\Delta\eta$ , can choose sign of  $\Delta\theta$
- can look like negative  $R_{56}$ 
  - get this for free by mixing two frequencies
  - single electrons at higher energy shift to front, but *regions* of high current are shifted back in phase

tunable: just cannot have  $R^{\text{FEL}} = 0$ , else  $b=0$

- bunching scales linear or better with  $R^{\text{FEL}}$

# Use EEHG to tolerate big energy offsets



beam: 2.4 GeV, 0.6  $\mu\text{m}$  emit, 150 keV  $\sigma_E$

200 nm seeds, 300 keV modulation

$R_1=7.5$  mm,  $R_2=280$  micron

optimum  $|R_2 - R_1 \lambda_x / \lambda_1| = 14$  micron (with energy spread)

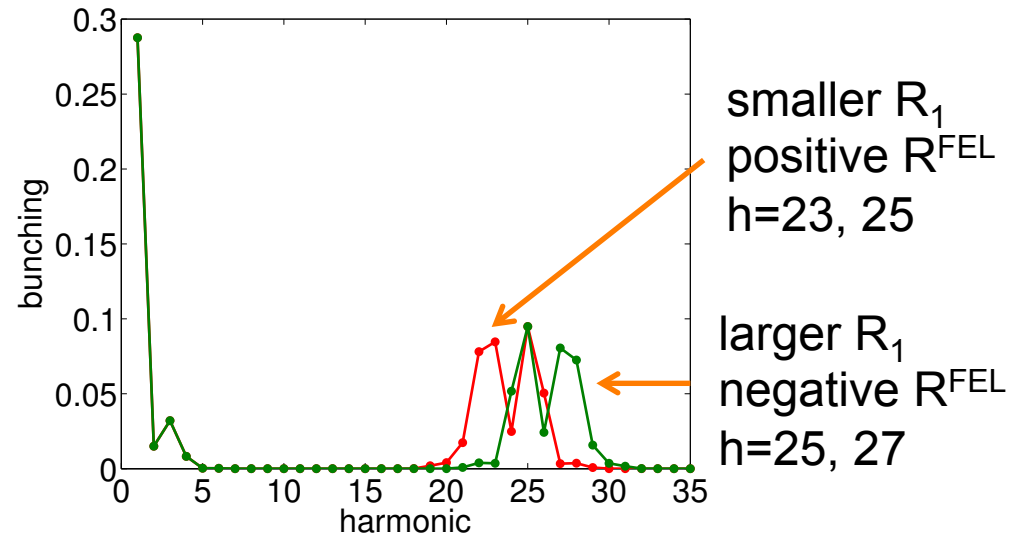
- close to HGHG case
- $\sim 1/10$  energy modulation

# Harmonics, bunching, and $R^{FEL}$

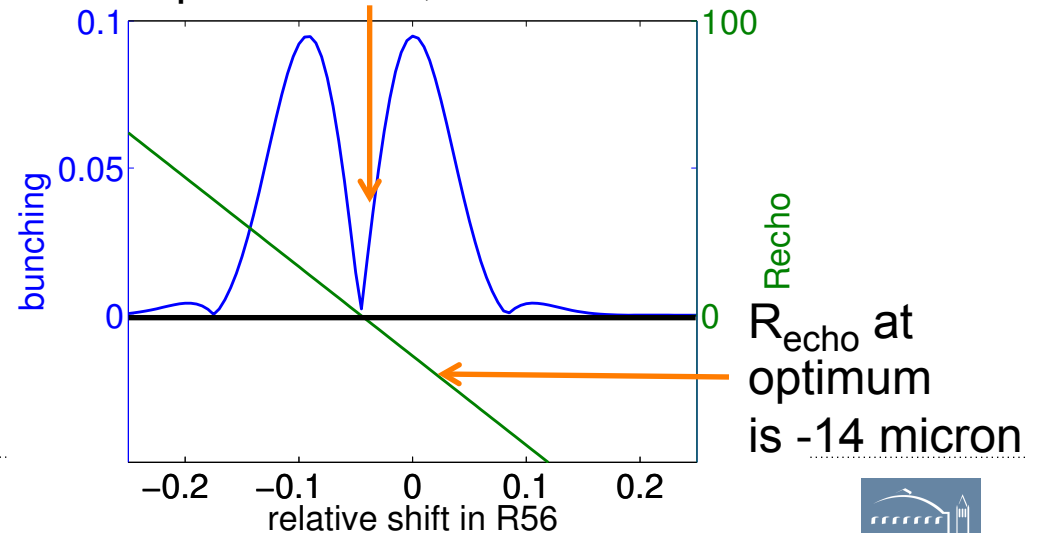
2 choices to optimize bunching:

25th harmonic, bunching and  $R^{FEL}$  vs  $\Delta R_1$   
 radiator adds 4  $\mu\text{m}$

includes energy spread  
 neglects scattering



will operate here, -5 micron

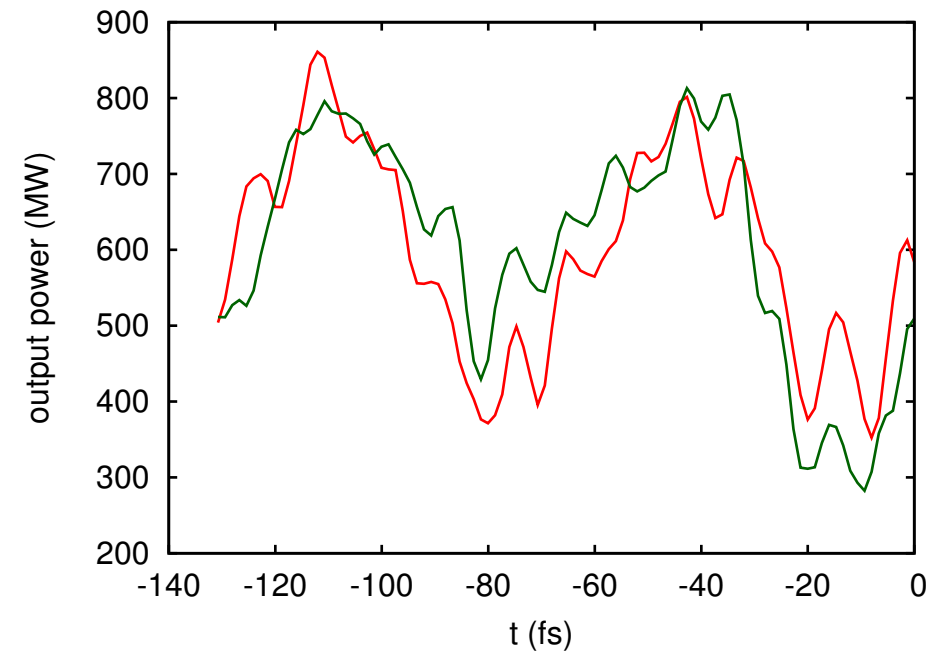
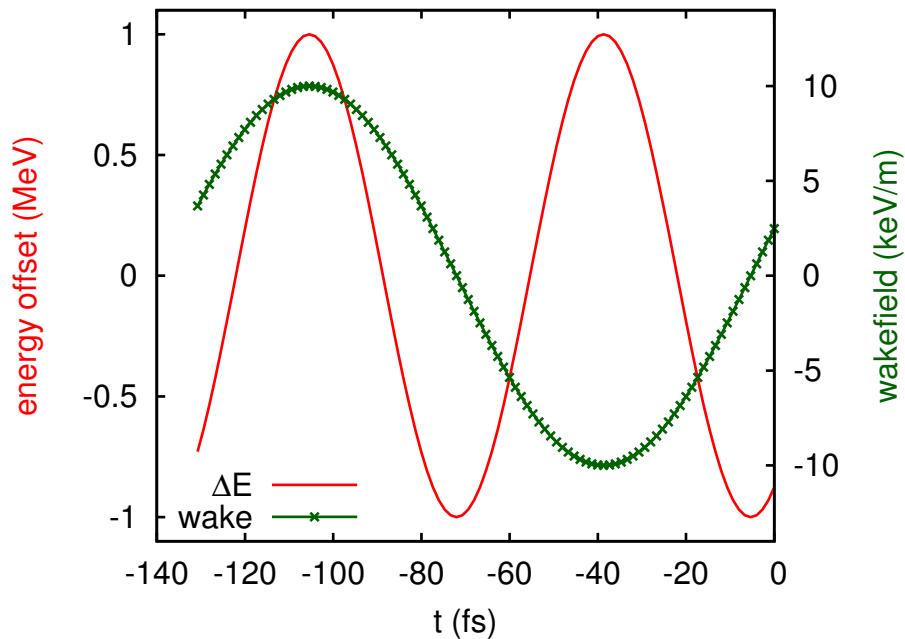


# EEHG simulations at 8 nm

consider initial energy modulation +/- 1 MeV

- optional +/- 10 keV/m wakefield

includes ISR and rough IBS models



red: just energy modulation    green: added wakefield

# Residual Phase Errors

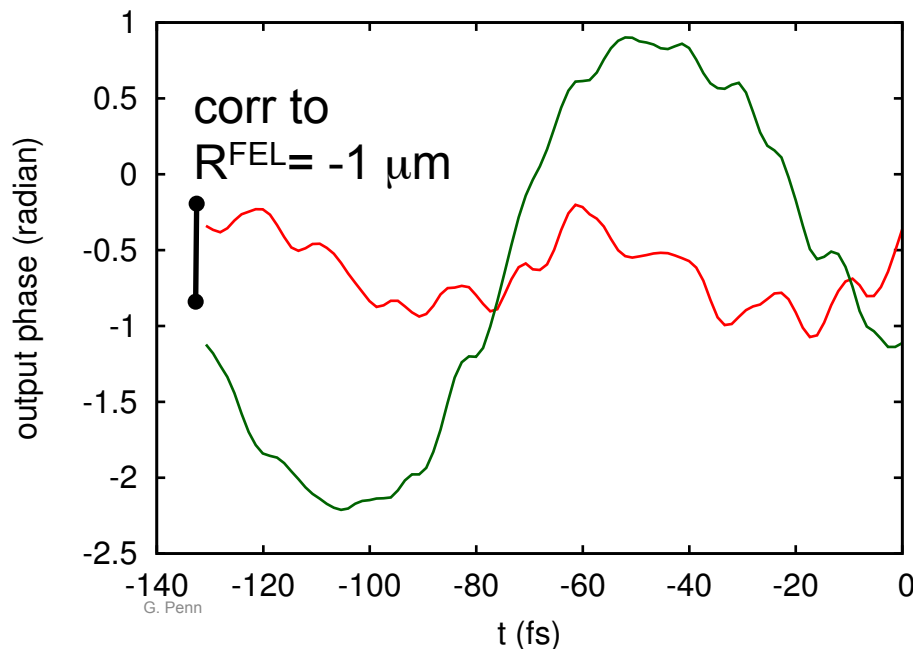
due to slippage, phase errors misaligned with energy

- but if slippage  $>$  modulation scale length, acts like  $\sigma_E$

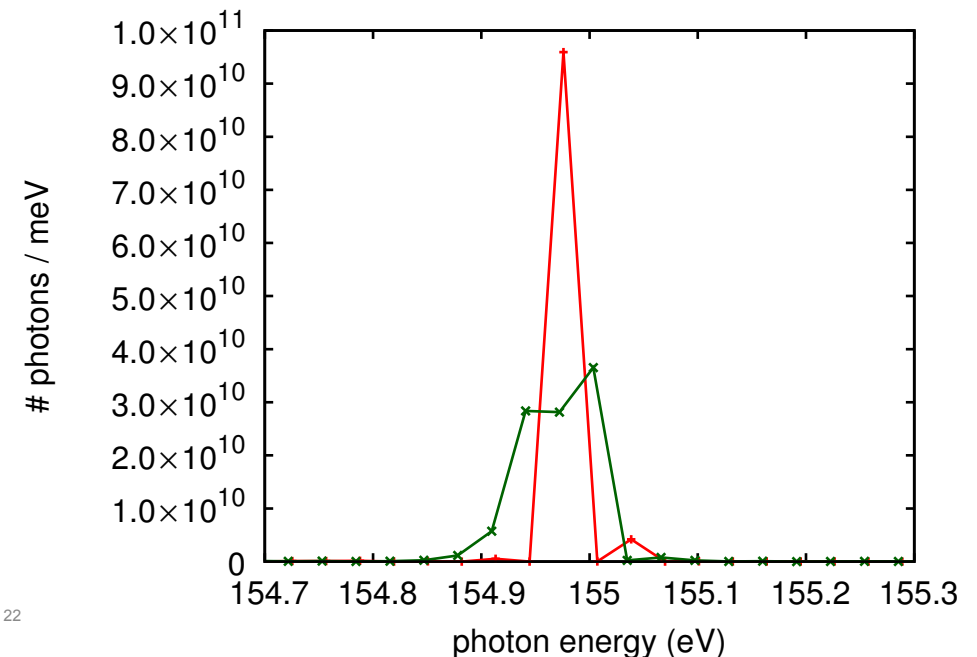
wakefields generate uncorrected phase errors

- thanks to Paul Emma for pointing this out

different radiated power generates extra energy offsets



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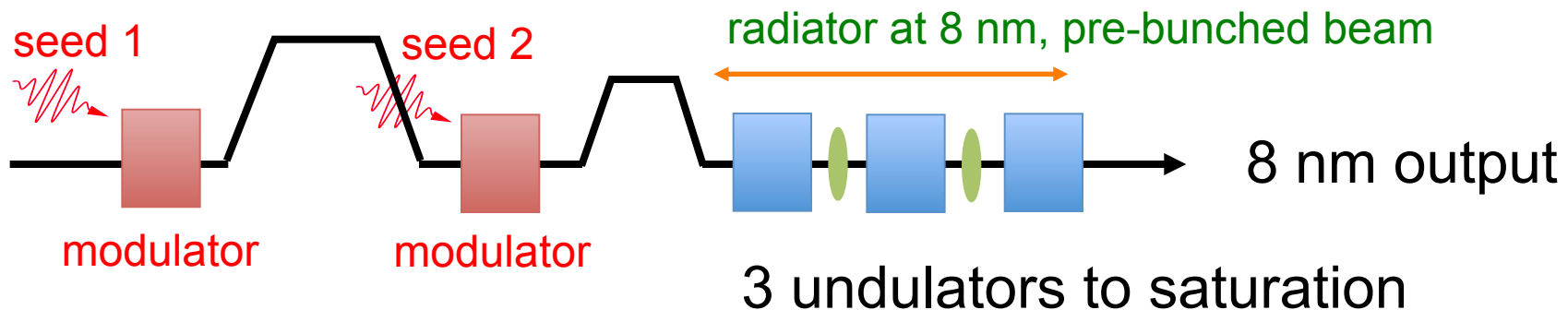
# Push to 2 nm

tweak design to reach 2 nm, using EEHG+HGHG

try not to use fresh bunch

- otherwise slice energy before/after uncorrelated
- could use fresh bunch and just accept phase offsets from after delay

earlier design

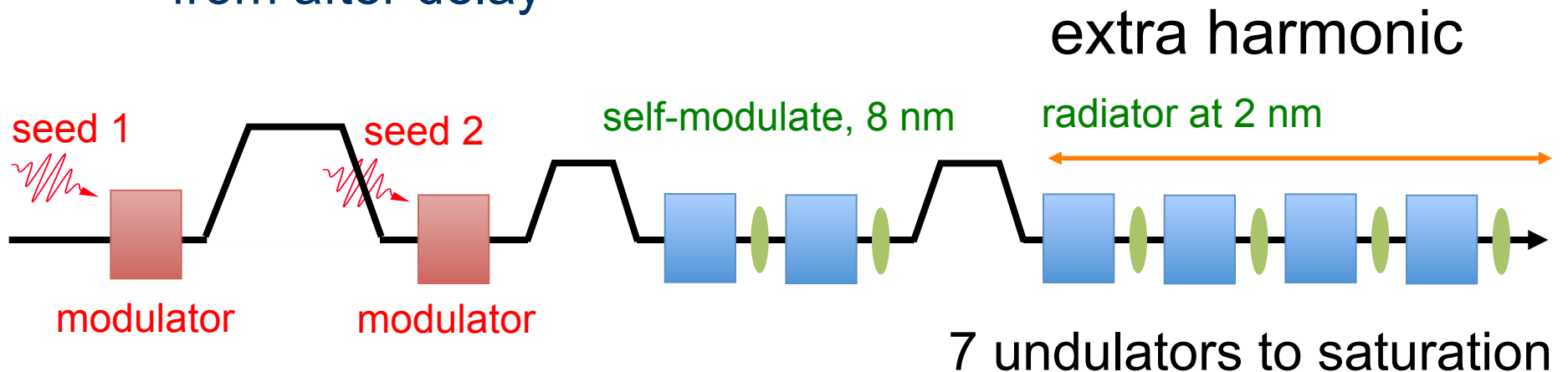


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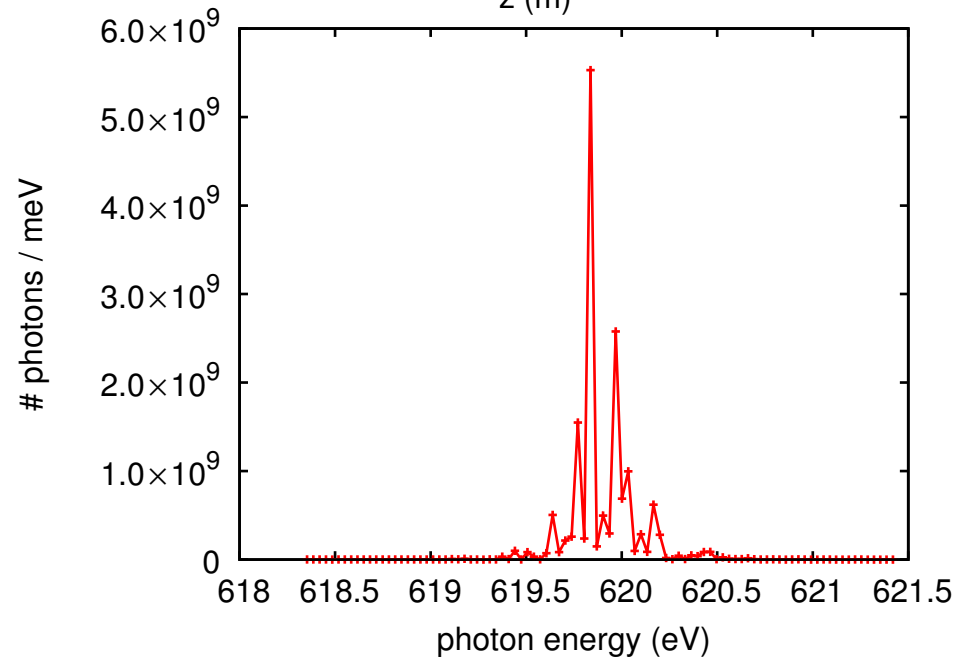
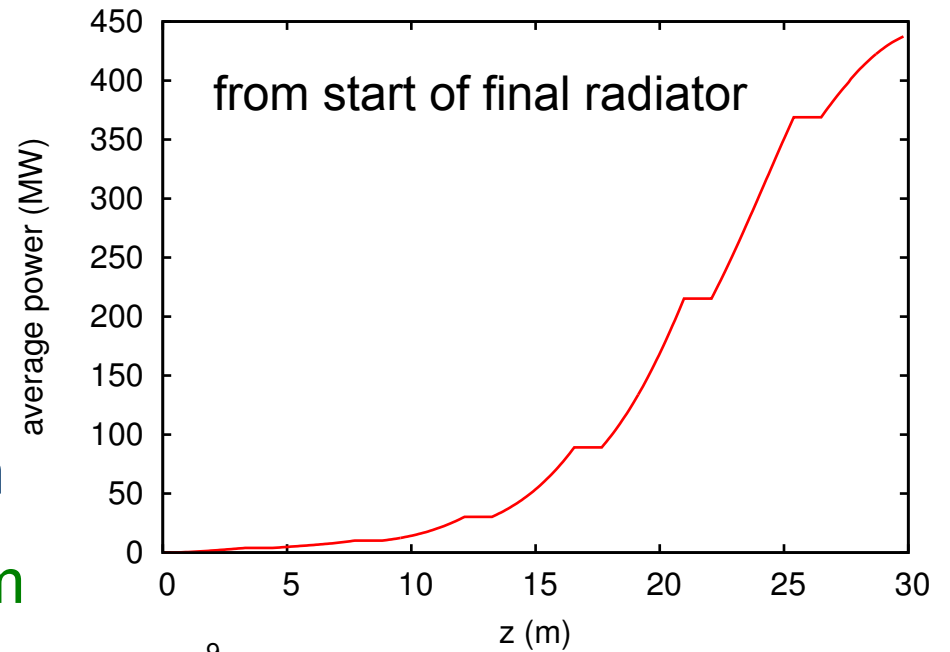
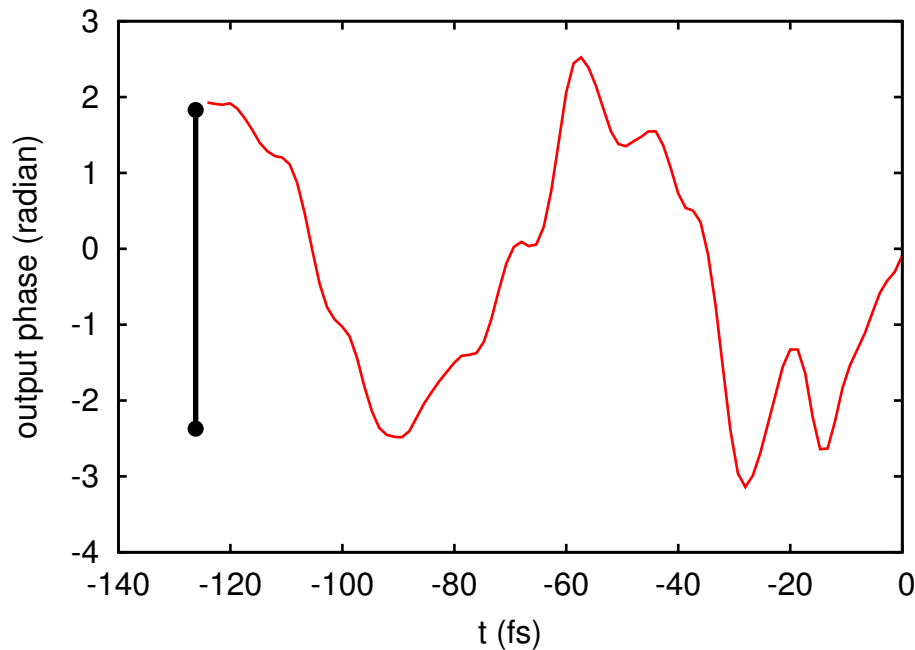


# Results at 2 nm

no wakes

equivalent to  $R^{\text{FEL}} \sim -1.5 \mu\text{m}$

compare to HGHG,  $23 \mu\text{m}$



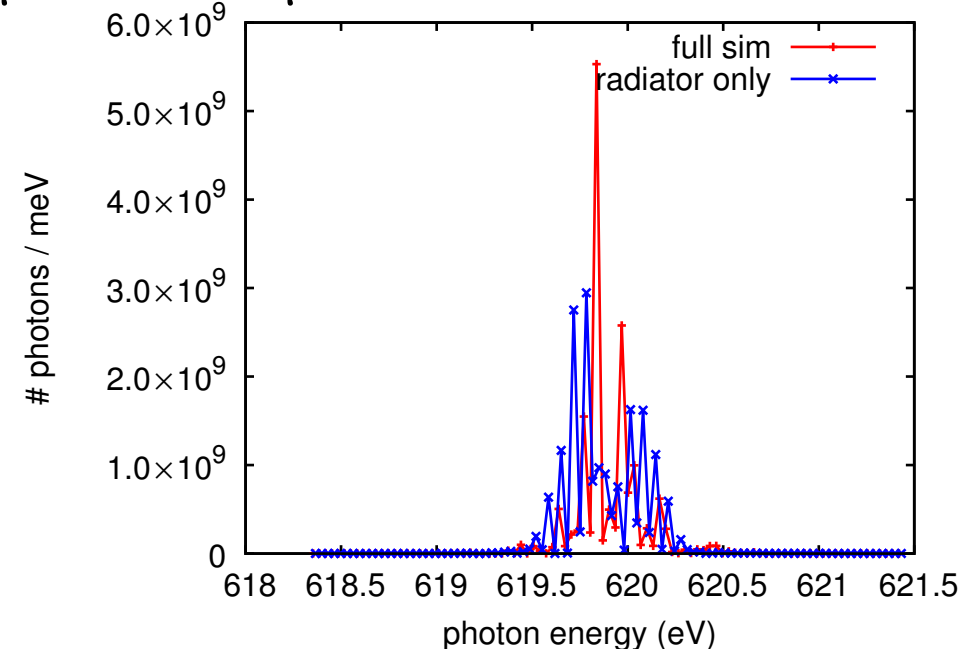
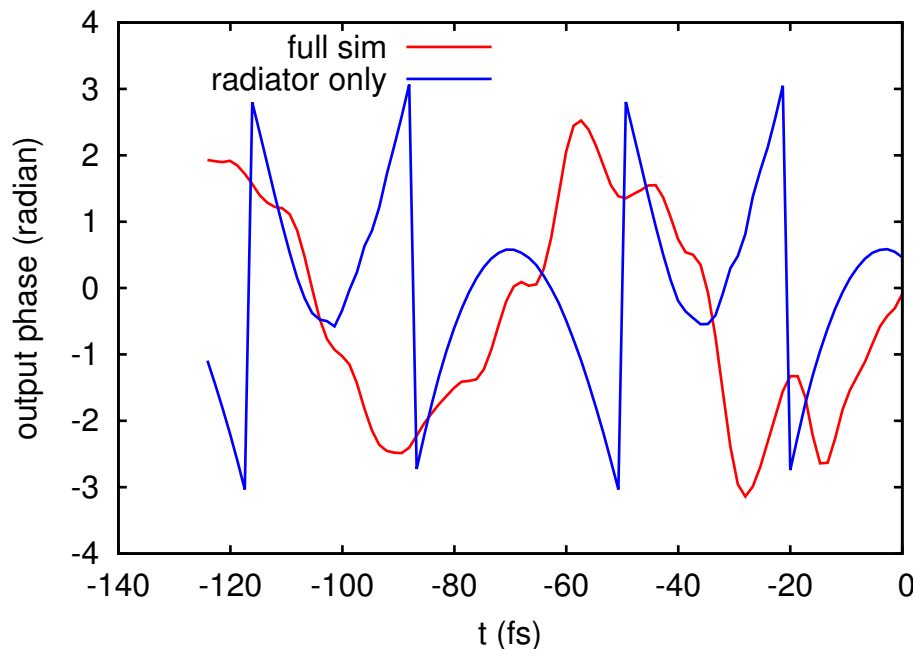
# Results at 2 nm

compare to “perfect” bunching at start of radiator

$R^{\text{FEL}}$  for radiator alone is  $\sim 3 \mu\text{m}$

improvement  $\sim \left| \sin(\pi L_{\text{shift}} / L_{\Delta E}) \right|$

3  $\mu\text{m}$       20  $\mu\text{m}$



# Quick Summary

rough scalings for different configurations:

- HGHG or OK,  $\Delta\theta \sim (\lambda_{\text{seed}}/\lambda_{\text{out}}) \Delta\eta/\eta_M > (\lambda_{\text{seed}}/\lambda_{\text{out}}) \Delta\eta/\rho$   
- want  $\Delta\eta < \rho / (\lambda_{\text{seed}}/\lambda_{\text{out}})$
- selfseed or radiator,  $\Delta\theta \sim (\# \text{ gain lengths}) \Delta\eta/3\rho$   
- want  $\Delta\eta < \rho \times 3 / (\# \text{ gain lengths})$
- EEHG,  $\Delta\theta \sim (\lambda_x/\lambda_{\text{out}}) \Delta\eta/\eta_{M1} \rightarrow \Delta\eta < \eta_{M1} (\lambda_{\text{out}}/\lambda_x)$
- other slice variations,  $\Delta\theta \sim (\# \text{ gain lengths}) \Delta\rho/3\rho$
- one region reaches saturation first:  $\sim 1$  radian  
- energy loss  $\sim \rho$  over a few gain lengths

slice energy spread barely has any effect

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G. Pellegrini “killer app” for echo scheme? 27